

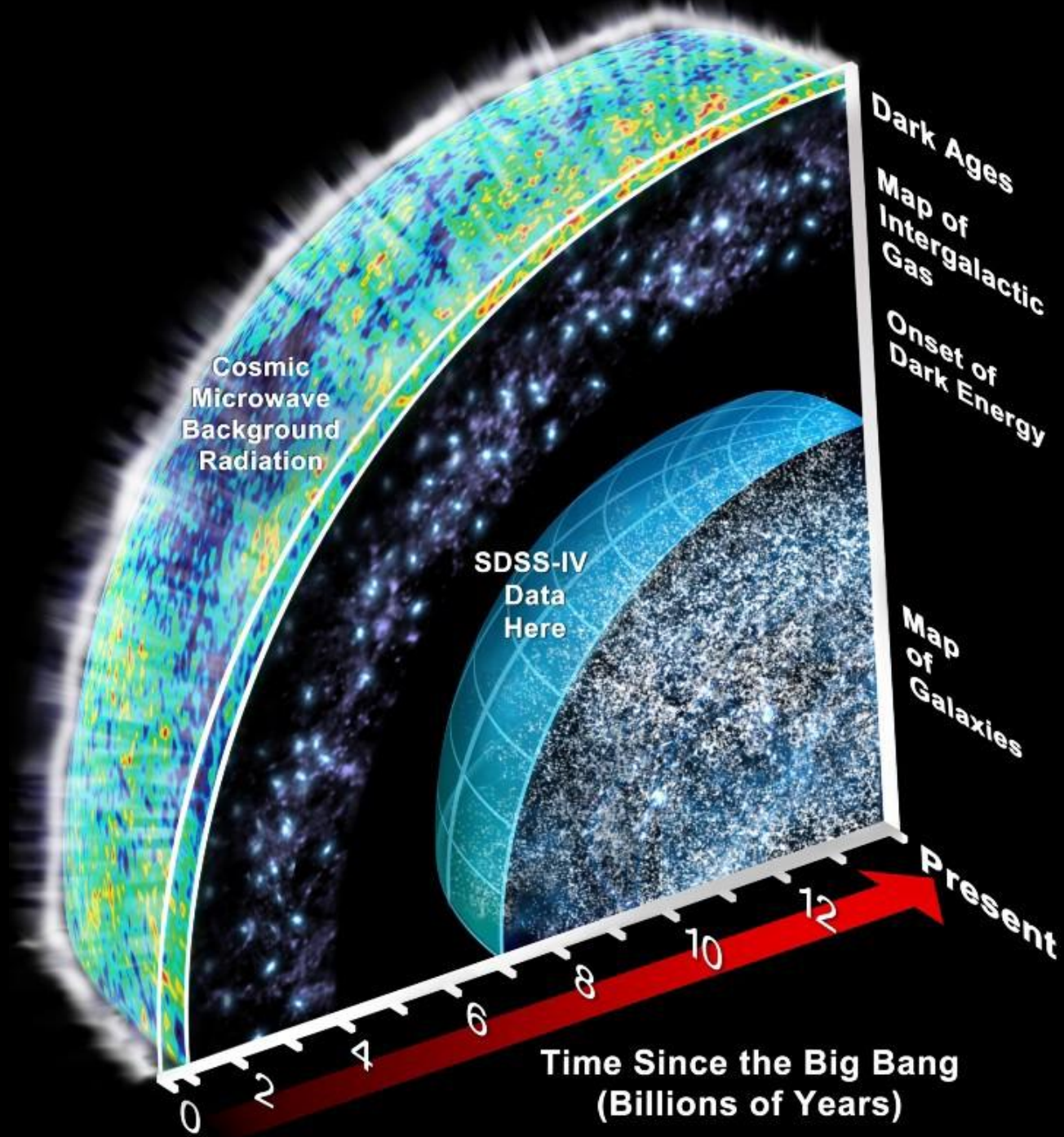
Intensity Mapping of $H\alpha$, $H\beta$, $[OII]$ and $[OIII]$ lines at $z < 5$

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Durban, 11/23/2016

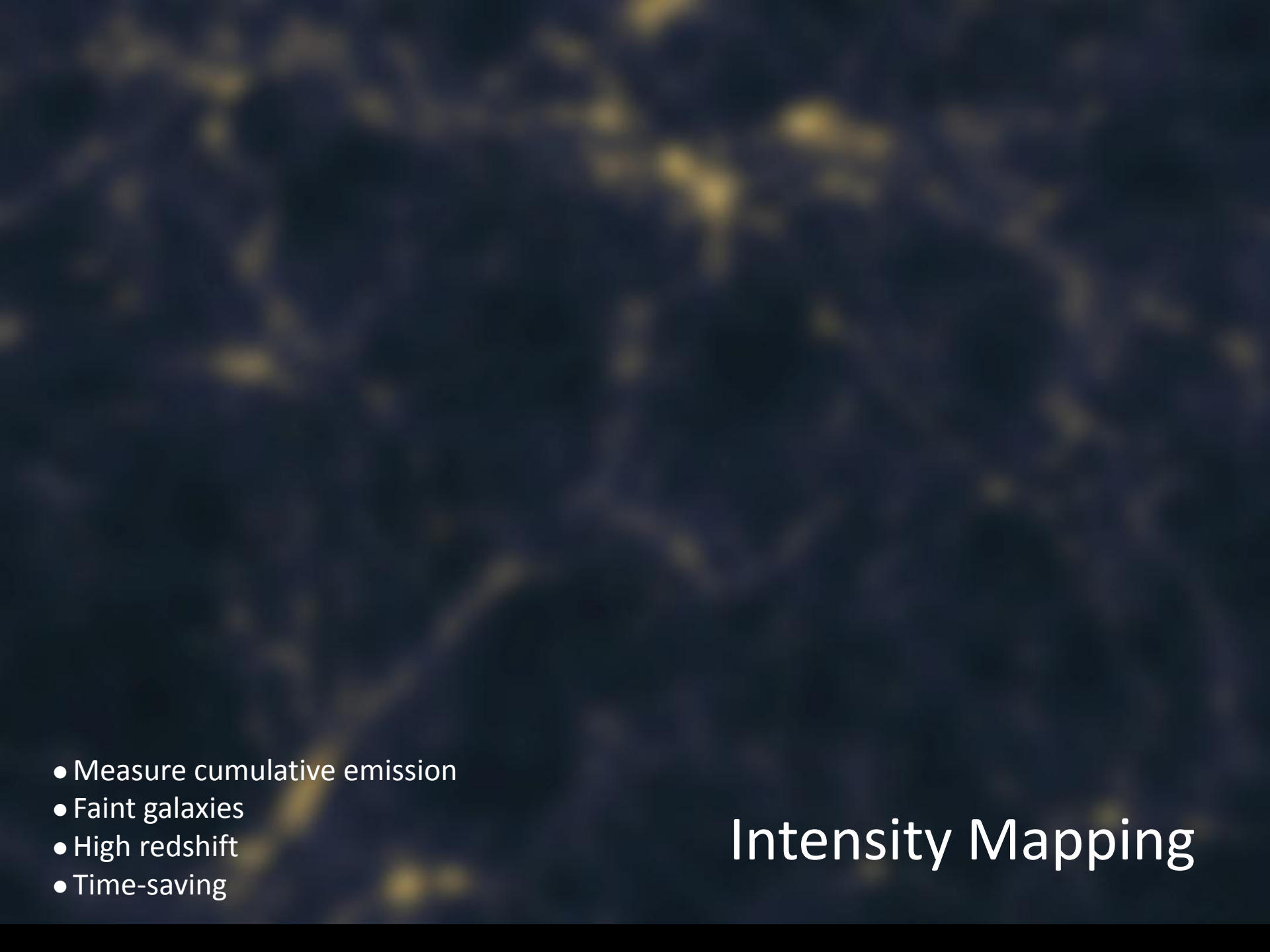
arXiv:1610.09060;

Collaborators: Asantha Cooray, Marta B. Silva, Michael Zemcov, Chang Feng,
Mario G. Santos, Olivier Dore, Xuelei Chen



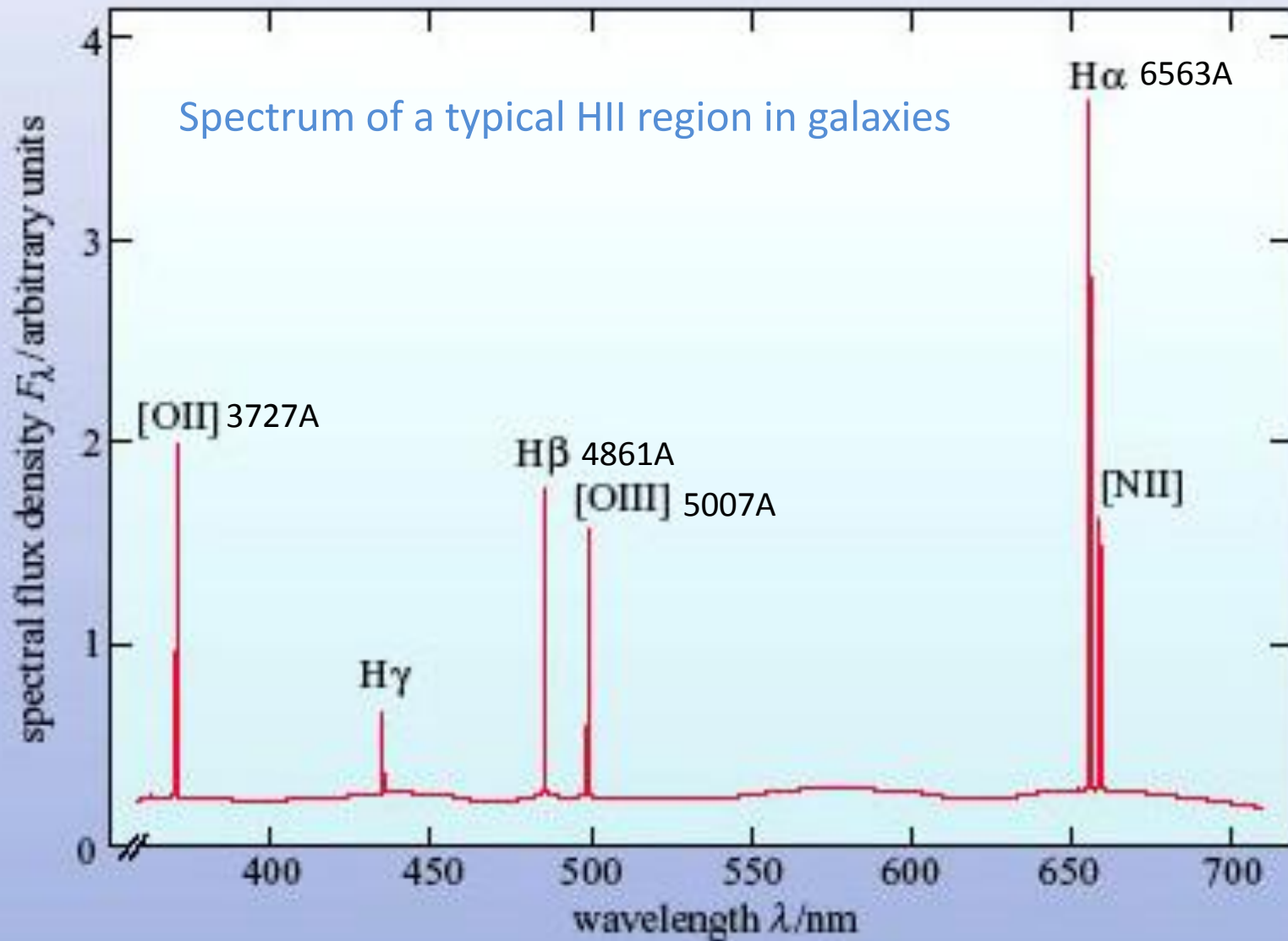
- 
- Resolve individual galaxies
 - Bright galaxies
 - Low redshift
 - Time-consuming

Galaxy Survey

- 
- The background of the slide is a Cosmic Microwave Background (CMB) fluctuation map, showing a complex pattern of yellow and orange spots against a dark blue background, representing temperature variations in the early universe.
- Measure cumulative emission
 - Faint galaxies
 - High redshift
 - Time-saving

Intensity Mapping

H α , H β , [OII] and [OIII] emission lines as IM tracers



Line luminosity function

- Observed LFs

$$\Phi(L)dL = \phi_* \left(\frac{L}{L_*} \right)^\alpha \exp \left(-\frac{L}{L_*} \right) \frac{dL}{L_*}$$

(Schechter function)

Dust extinction included!

- SFR simulations (Guo et al 2013)

$$\text{SFR}(M) = 10^a \left(\frac{M}{M_1} \right)^b \left(1 + \frac{M}{M_2} \right)^c$$

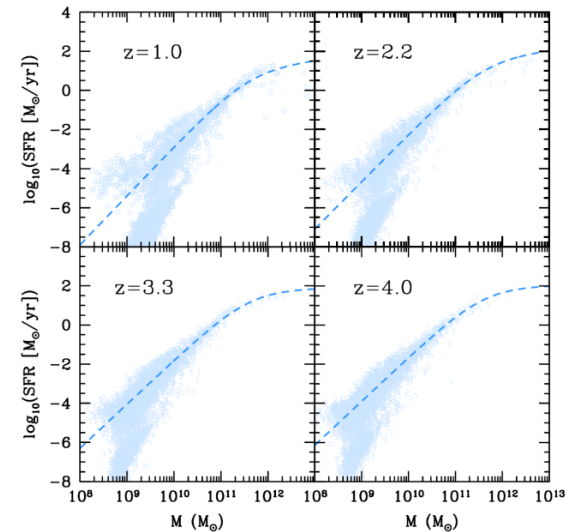
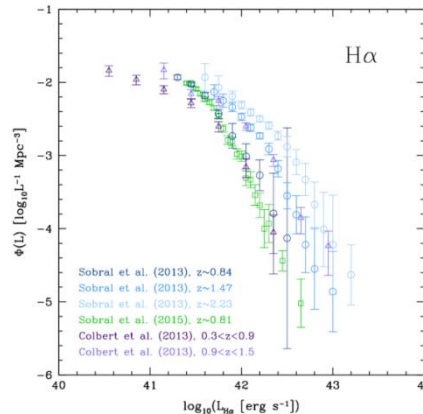


- SFRD function from Obs.

(Hopkins & Beacom 2006; Madau & Dickinson 2014)

$$\text{SFRD}(z) = \int dM (dn/dM) \text{SFR}(M, z) \Rightarrow \text{SFR}(M, z) = f_*(z) \frac{\Omega_b}{\Omega_M} \frac{1}{t_s} M$$

$A_{\text{H}\alpha} = 1.0 \text{ mag}$, $A_{[\text{OIII}] } = 1.32 \text{ mag}$, $A_{[\text{OII}]} = 0.62 \text{ mag}$, and $A_{\text{H}\beta} = 1.38$



$$\begin{aligned} \text{SFR}(M_\odot \text{yr}^{-1}) &= (7.9 \pm 2.4) \times 10^{-42} L_{\text{H}\alpha}, \\ \text{SFR}(M_\odot \text{yr}^{-1}) &= (7.6 \pm 3.7) \times 10^{-42} L_{[\text{OIII}]}, \\ \text{SFR}(M_\odot \text{yr}^{-1}) &= (1.4 \pm 0.4) \times 10^{-41} L_{[\text{OII}]}. \end{aligned}$$



Line mean intensity and power spectrum

- Line mean intensity

$$\bar{I}_\nu(z) = \int_{L_{\min}}^{L_{\max}} dL \Phi(L) \frac{L}{4\pi D_L^2} y(z) D_A^2 \quad (\text{For LFs})$$

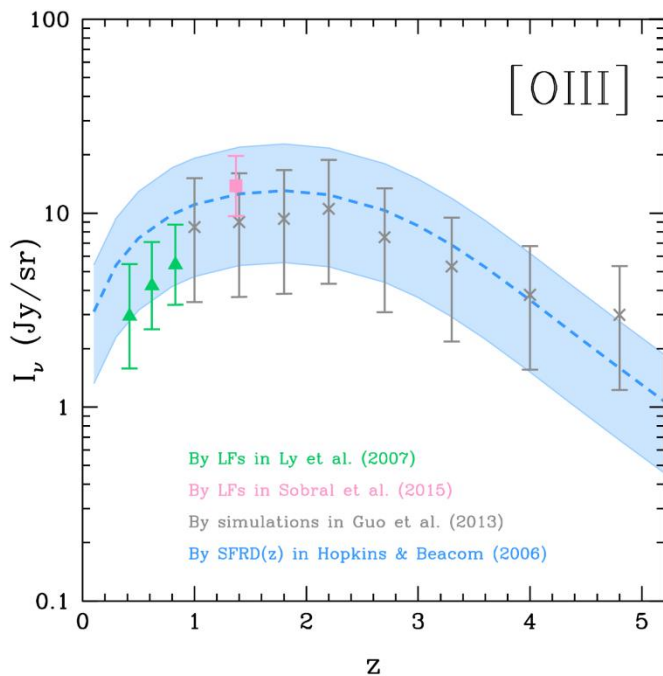
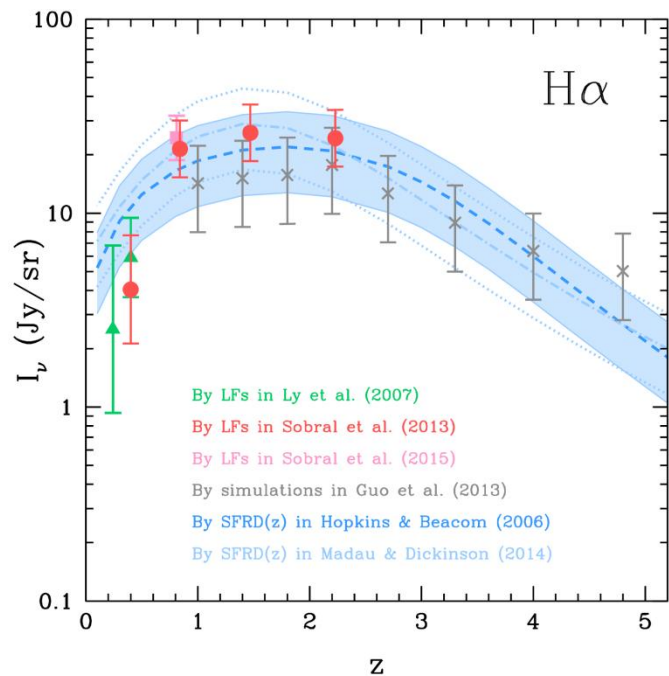
$$\bar{I}_\nu(z) = \int_{M_{\min}}^{M_{\max}} dM \frac{dn}{dM} \frac{L_{\text{line}}(M, z)}{4\pi D_L^2} y(z) D_A^2 \quad (\text{For SFR})$$

- Line intensity power spectrum:

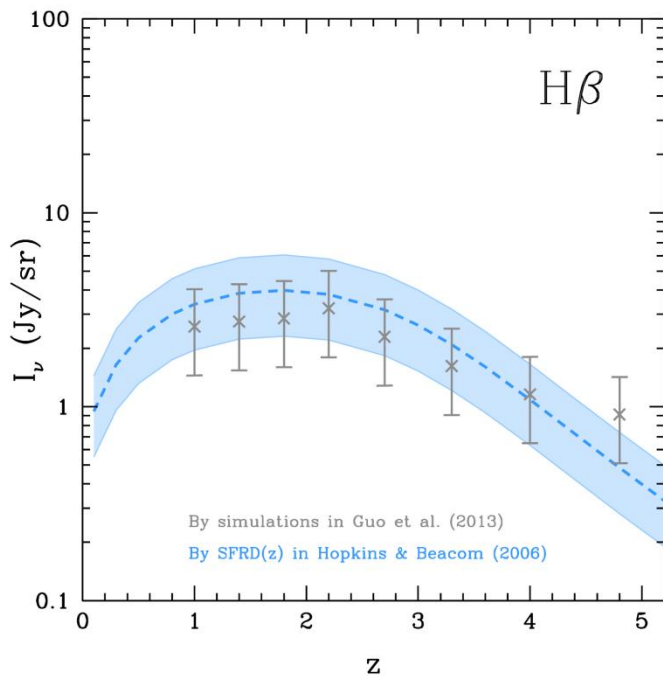
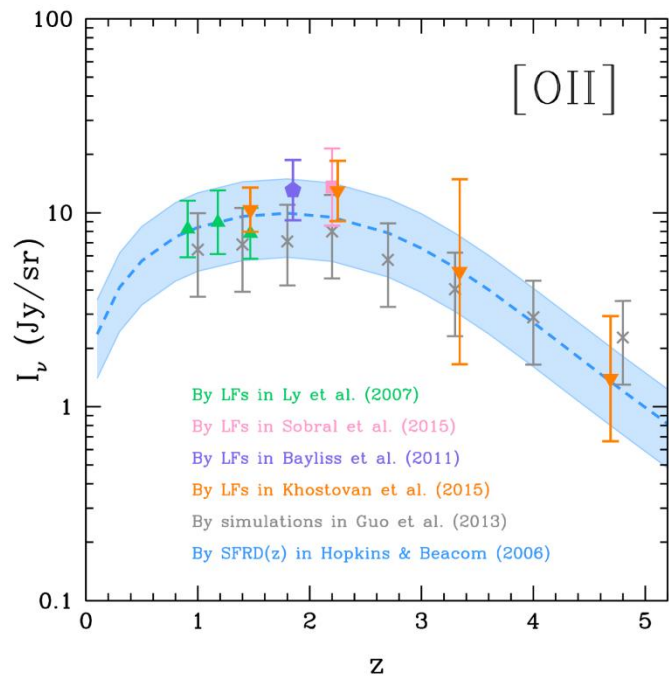
$$P_{\text{line}}^{\text{clus}}(k, z) = \bar{b}_{\text{line}}^2 \bar{I}_{\text{line}}^2 P_{\delta\delta}(k, z) \quad (\text{Clustering power})$$

$$P_{\text{line}}^{\text{shot}}(z) = \int_{M_{\min}}^{M_{\max}} dM \frac{dn}{dM} \left[\frac{L_{\text{line}}}{4\pi D_L^2} y(z) D_A^2 \right]^2 \quad (\text{Shot-noise power})$$

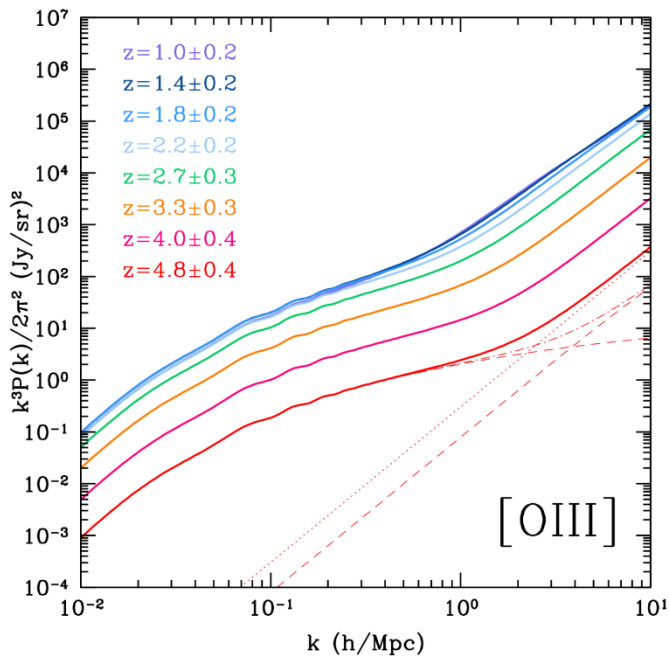
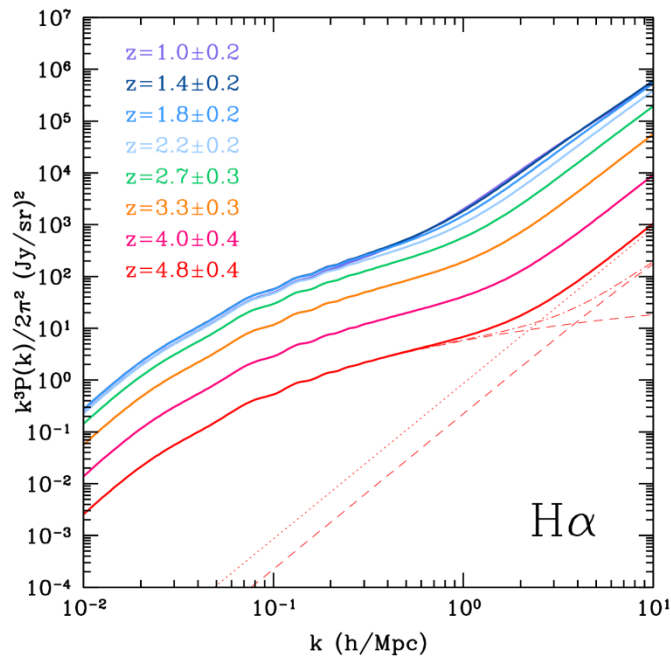
$$\bar{b}_{\text{line}}(z) = \frac{\int_{M_{\min}}^{M_{\max}} dM \frac{dn}{dM} L_{\text{line}} b(M, z)}{\int_{M_{\min}}^{M_{\max}} dM \frac{dn}{dM} L_{\text{line}}} \quad (\text{line bias})$$



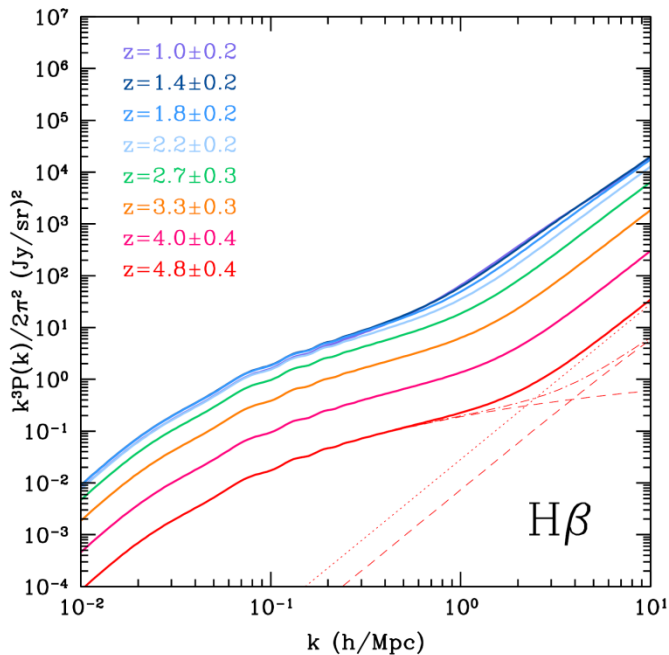
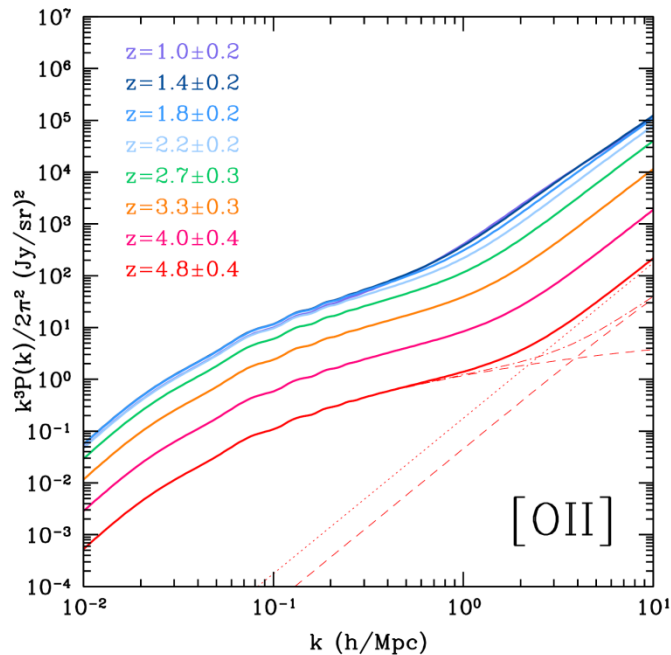
Line mean
intensity at
 $0 < z < 5$



$H\alpha > [OIII] > [OII] > H\beta$



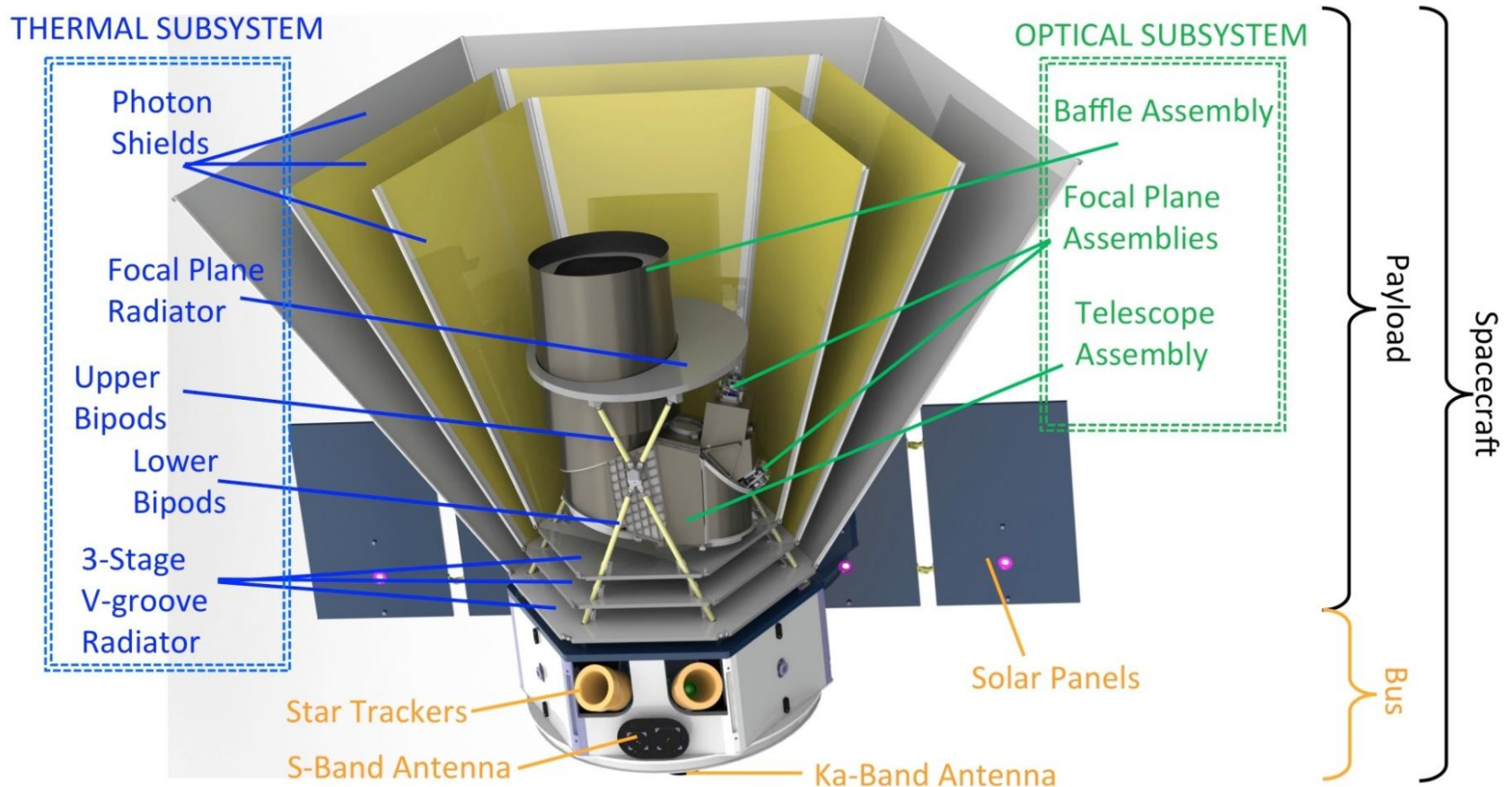
Line intensity
power spectra
at $1 < z < 5$



$H\alpha > [OIII] > [OII] > H\beta$
at the same z

Detectability

SPHEREx experiment



Credit: <http://spherex.caltech.edu/>

A small NASA space explore mission



SPHEREx instrument parameters

Telescope Effective Aperture	20 cm
Pixel Size	6.2" x 6.2"
Field of View	2 x (3.5° x 7.0°); dichroic
Resolving Power and Wavelength Coverage	λ = 0.75- 4.18 μ m; R=41.4 λ = 4.18 - 5.00 μ m; R=135
Arrays	2x Hawaii-2RG 2.5 μ m 2x Hawaii-2RG 5.3 μ m
Point Source Sensitivity	18.4 AB mag (5 σ) per frequency bin referenced at 2 μ m. Sensitivity has 380% total margin to science requirement
Cooling	All-Passive
2.5 μ m Array and Optics Temperature	80K
5.3 μ m Array Temperature	55K
Payload Mass	68.7 kg

- Foreground line contamination:

$$P_{\text{obs}}(k, z) = P_s(k, z) + \sum_{i=1}^N P_f^{p,i}(k_f, z) \quad (\text{Total power spectrum})$$

$$P_f^p(k_f, z) = A_{\perp}^2 A_{\parallel} P_f(k_f, z_f) \quad (\text{Foreground line power spectrum})$$

$$k = \sqrt{k_{\perp}^2 + k_{\parallel}^2} \quad k_f = \sqrt{A_{\perp}^2 k_{\perp}^2 + A_{\parallel}^2 k_{\parallel}^2}$$

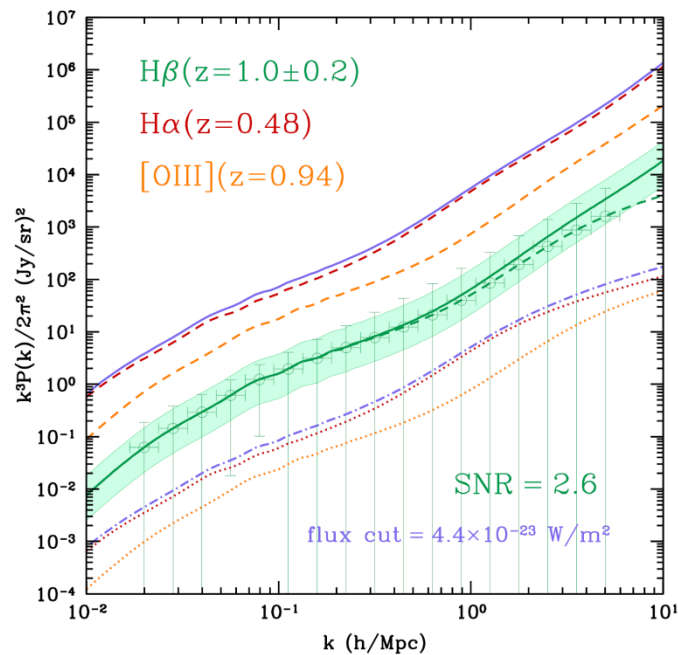
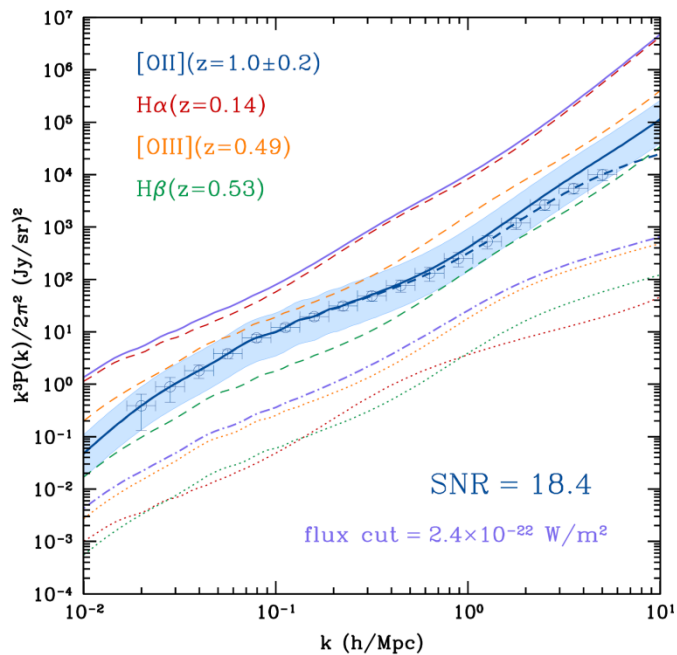
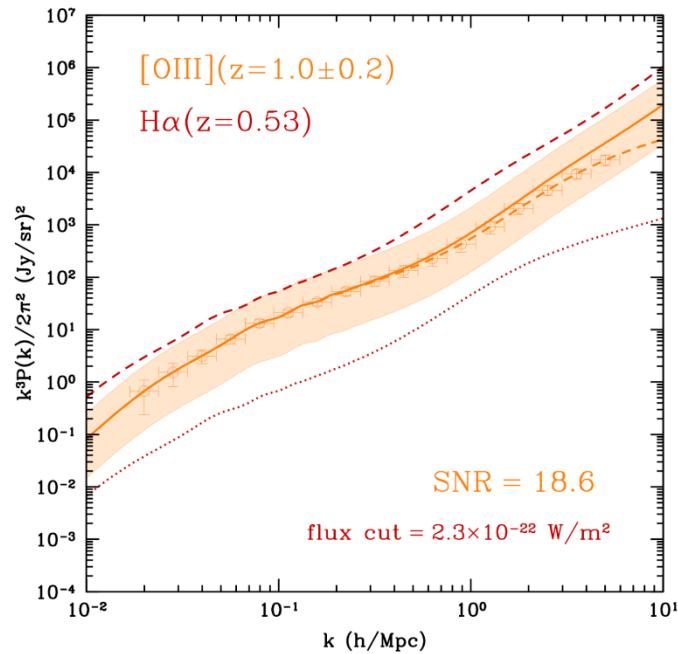
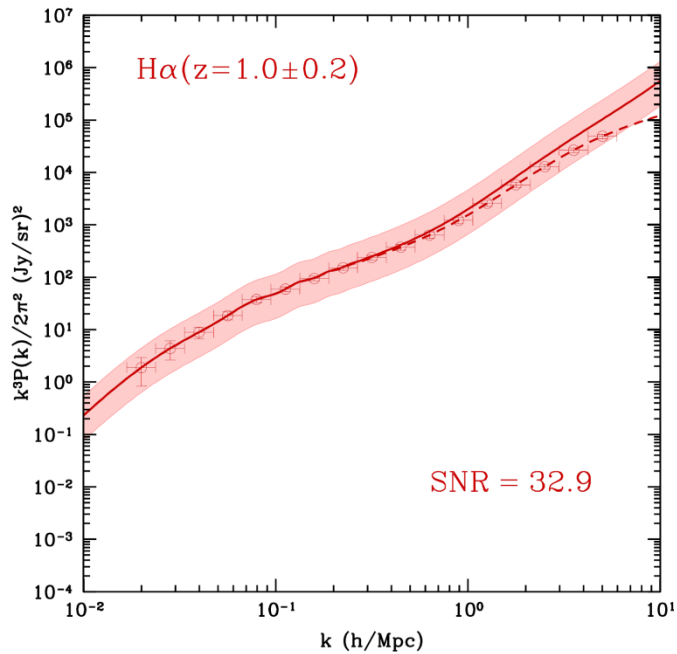
$$A_{\perp} = r_s/r_f \quad A_{\parallel} = y_s/y_f$$

- Detected Signal to Noise Ratio (SNR):

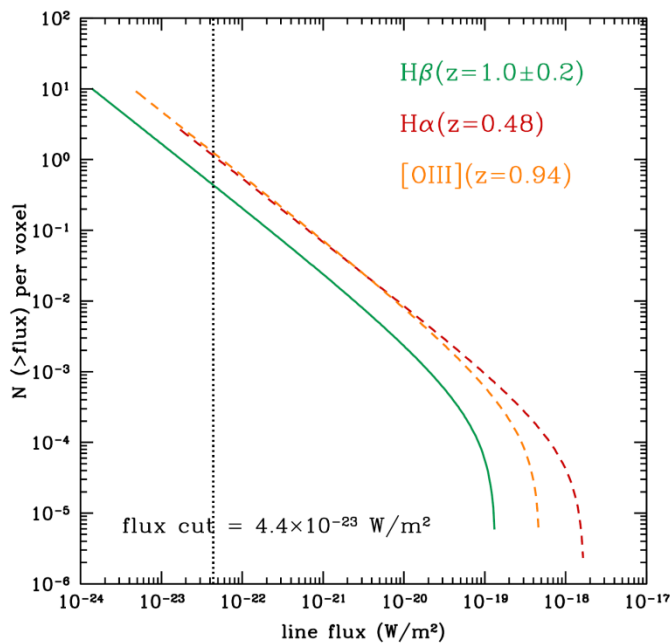
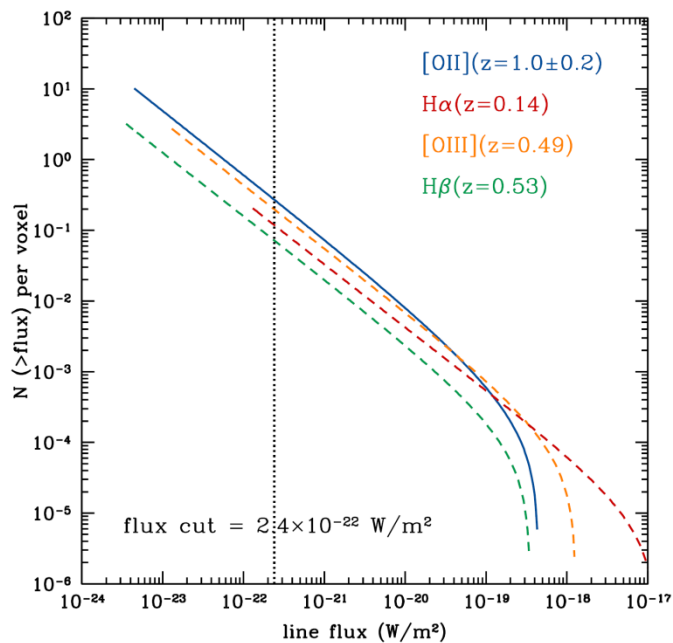
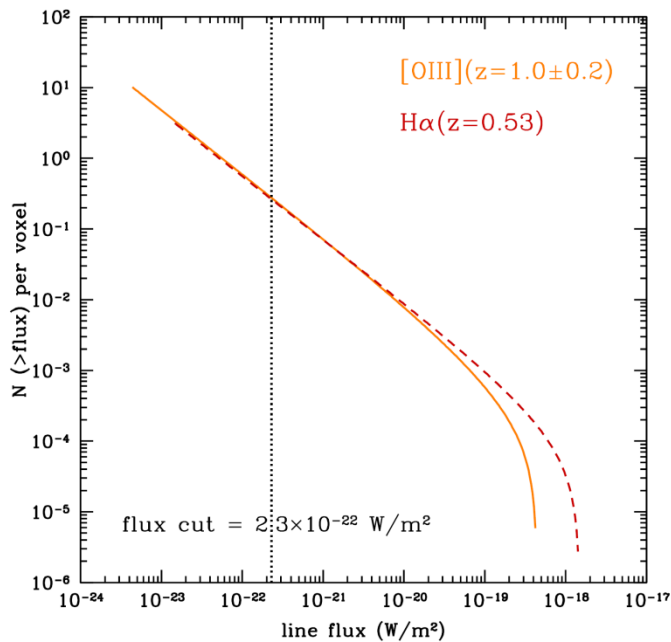
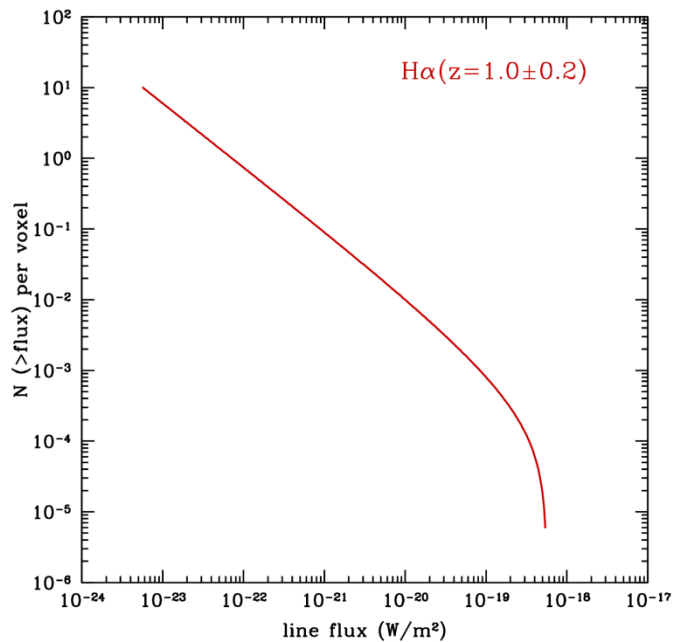
$$\Delta P_{\text{line}}(k)^2 = \frac{[P_{\text{line}}(k) + P_N^{\text{line}}(k)]^2}{N_m(k)} \quad (\text{Variance of the power spectrum})$$

$$P_N^{\text{line}}(k) = \frac{V_{\text{pix}} \sigma_{\text{pix}}^2}{t_{\text{pix}}} \quad (\text{noise power spectrum})$$

$$\text{SNR} = \sqrt{\sum_{k \text{ bin}} \left[\frac{P_{\text{line}}(k)}{\Delta P_{\text{line}}(k)} \right]^2}$$



Detectability of
line intensity
power spectra
at $z \sim 1$



Number of
sources per
voxel at $z \sim 1$

SNRs, flux cuts, and % of removed pixels for SPHEREx

Line		$z \sim 1.0$	$z \sim 1.4$	$z \sim 1.8$	$z \sim 2.2$	$z \sim 2.7$	$z \sim 3.3$	$z \sim 4.0$	$z \sim 4.8$
H α	SNR	32.9	44.0	33.6	29.4	39.6	20.0	7.1	1.3
	flux cut (W/m ²)	-	-	-	-	-	-	-	-
	% of rem. pix.	-	-	-	-	-	-	-	-
[OIII]	SNR	18.6	13.0	19.7	14.4	11.5	4.8	2.6	0.5
	flux cut (W/m ²)	2.3×10^{-22}	1.4×10^{-22}	8.4×10^{-23}	6.0×10^{-23}	2.4×10^{-23}	6.8×10^{-24}	2.8×10^{-24}	1.3×10^{-24}
	% of rem. pix.	3%	4%	5%	6%	10%	21%	42%	55%
[OII]	SNR	18.4	11.4	8.2	6.4	8.4	3.2	0.8	0.1
	flux cut (W/m ²)	2.4×10^{-22}	8.6×10^{-23}	4.0×10^{-23}	2.5×10^{-23}	9.9×10^{-24}	4.6×10^{-24}	2.4×10^{-24}	9.9×10^{-25}
	% of rem. pix.	3%	5%	9%	20%	32%	43%	53%	67%
H β	SNR	2.6	1.8	2.9	2.1	1.4	0.5	0.3	< 0.1
	flux cut (W/m ²)	4.4×10^{-23}	2.6×10^{-23}	1.3×10^{-23}	9.2×10^{-24}	5.2×10^{-24}	3.0×10^{-24}	1.6×10^{-24}	8.8×10^{-25}
	% of rem. pix.	12%	15%	21%	27%	38%	48%	65%	87%

- H α is the best tracer (no strong interloper lines, SNR>7 at $z<4$)
- [OIII] is better than [OII] (SNR_[OIII]>11 and SNR_[OII]>8 at $z<3$)
- H β is challenging to measure (strong contamination, SNR<3 for all z)

Cross correlation with 21-cm line

CHIME and Tianlai 21-cm experiments



CHIME and Tianlai specs

	CHIME	Tianlai	Unit
Survey area A_s	10000	10000	deg ²
Total int. time t_{tot}	10^4	10^4	hour
Total bandwidth	400-800	400-1420	MHz
Redshift range	0.8-2.5	0.0-2.5	-
Sys. Temp. T_{sys}	50	50	K
FoV N-S	~ 150	~ 150	deg
FoV E-W	~ 1.9	~ 1.6	deg
Cylinder size	100×20	120×15	m ²
Num. of cylinders	5	8	-
Tot. Collecting area	10000	14400	m ²
Num. of feeds	256×5	275×8	-
Freq. resolution $\Delta\nu$	~ 1	~ 0.1	MHz

- Cross power spectrum:

$$P_{\text{cross}}^{\text{clus}}(k, z) = \bar{b}_{21\text{cm}} \bar{b}_{\text{line}} \bar{T}_{21\text{cm}} \bar{T}_{\text{line}} P_{\delta\delta}(k, z) \quad (\text{Cross clustering power})$$

$$P_{\text{cross}}^{\text{shot}} = \sqrt{P_{\text{line}}^{\text{shot}} P_{21\text{cm}}^{\text{shot}}} \quad (\text{Cross shot-noise power})$$

$$P_{21\text{cm}}^{\text{shot}}(z) = \int_{M_{\text{min}}}^{M_{\text{max}}} dM \frac{dn}{dM} \left(\bar{T}_{21\text{cm}} \frac{M_{\text{HI}}}{\rho_{\text{HI}}} \right)^2 \quad (\text{21-cm shot-noise power})$$

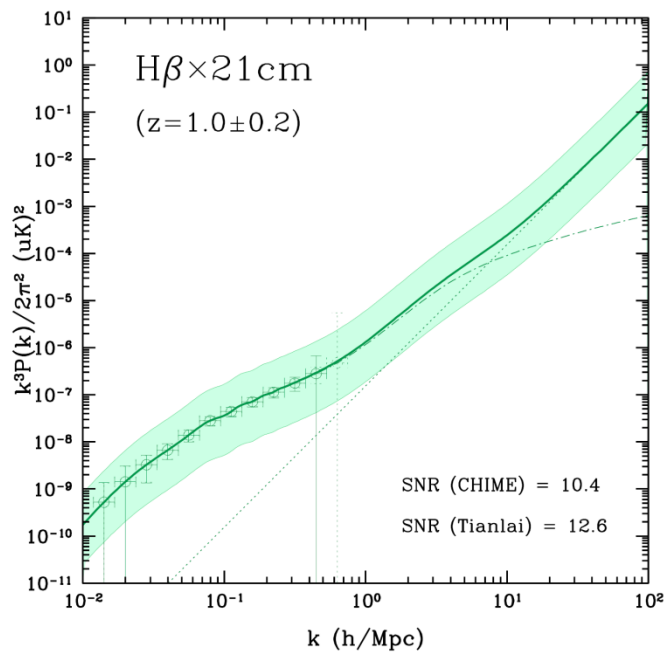
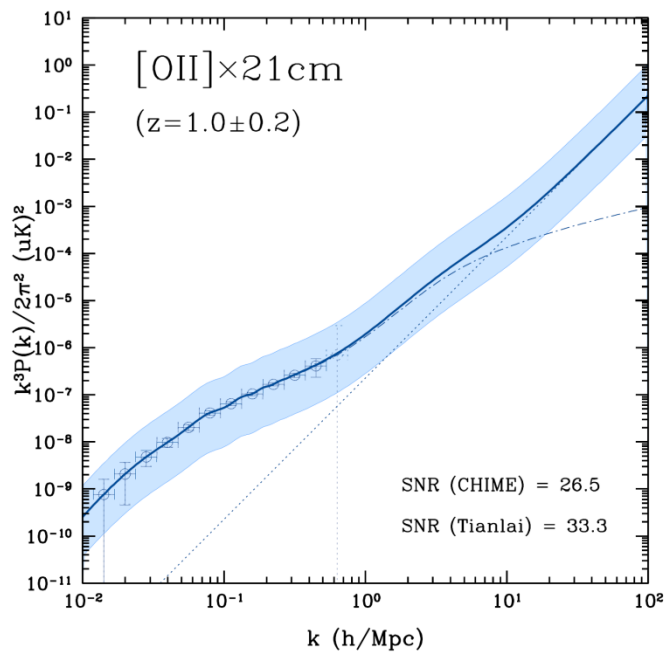
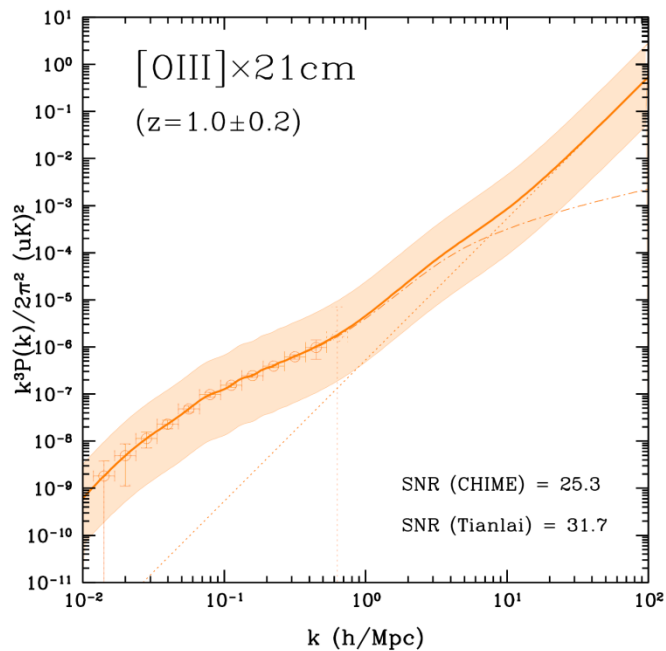
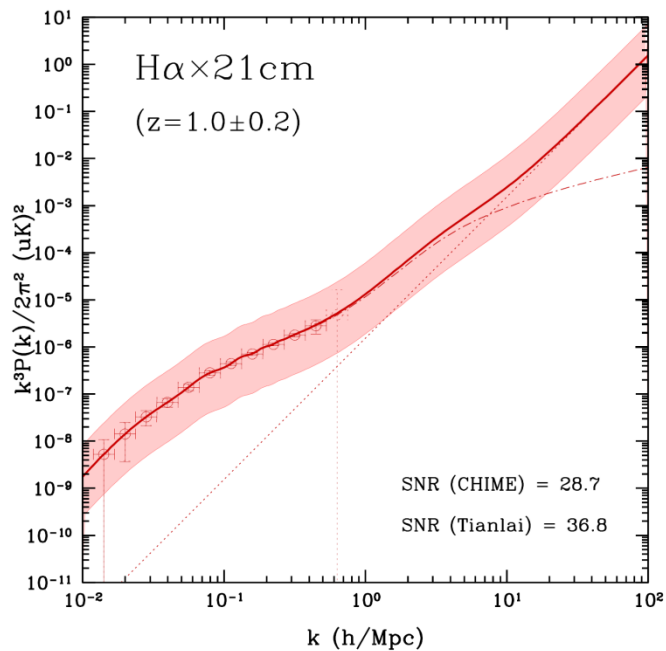
$$\bar{b}_{21\text{cm}}(z) = \frac{\int_{M_{\text{min}}}^{M_{\text{max}}} dM \frac{dn}{dM} M_{\text{HI}} b(M, z)}{\rho_{\text{HI}}} \quad \bar{T}_{21\text{cm}}(z) = 248 \left(\frac{\Omega_{\text{HI}}}{10^{-3}} \right) \left(\frac{h}{0.73} \right) \left(\frac{1+z}{1.8} \right)^{0.5} \left[\frac{\Omega_M + \Omega_\Lambda (1+z)^{-3}}{0.37} \right]^{-0.5} \mu\text{K}.$$

- Variance of the cross power spectrum:

$$(\Delta P_{\text{cross}})^2 = \frac{P_{\text{cross}}^2 + (P_{\text{line}} + P_N^{\text{line}})(P_{21\text{cm}} + P_N^{21\text{cm}})}{2 N_m^{\text{cross}}(k)} \quad (\text{Variance})$$

$$P_N^{21\text{cm}} = r_c^2 y(z) \frac{\lambda^2 T_{\text{sys}}^2}{A_e t_k} \quad (\text{21-cm noise power spectrum})$$

$$t_k = t_0 (A_e / \lambda^2) n(\mu_\perp) \quad \mu_\perp = k \sin(\theta) r_c / 2\pi$$



Cross power
spectra of
optical lines
and 21-cm line
at $z \sim 1$

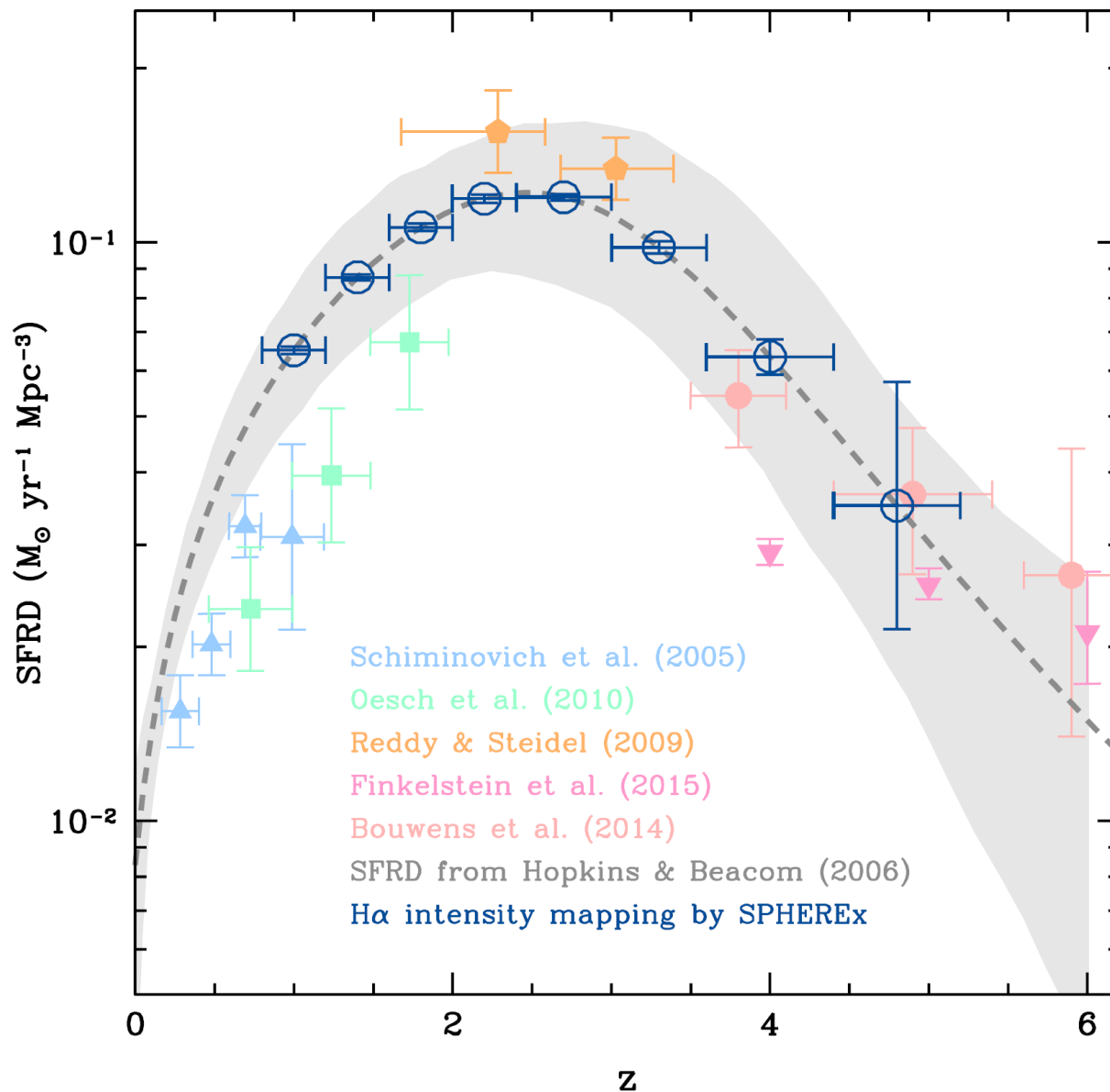
SNRs of SPHEREx $\times$ CHIME and Tianlai

Line	21-cm expt.	$z = 1.0 \pm 0.2$	$z = 1.4 \pm 0.2$	$z = 1.8 \pm 0.2$	$z = 2.2 \pm 0.2$
$H\alpha$	$\times$ CHIME	28.7	26.9	18.9	15.2
	$\times$ Tianlai	36.8	36.1	26.6	22.0
[OIII]	$\times$ CHIME	25.3	16.7	17.8	12.2
	$\times$ Tianlai	31.7	21.6	18.4	17.4
[OII]	$\times$ CHIME	26.5	17.2	11.7	8.8
	$\times$ Tianlai	33.3	22.2	15.8	12.4
$H\beta$	$\times$ CHIME	10.4	6.8	7.8	5.2
	$\times$ Tianlai	12.6	8.5	10.5	7.3

HIRAX has similar SNR; SKA1-mid as single dishes has smaller SNR (SNR $\sim$ 5.7 at $z=1$)

Cross correlation is a good method for extracting IM signal!

Constraints on SFRD(z) by SPHEREx



Error < 7% at $z < 4$,
better than the
measurements
from galaxy LFs

Derived by Fisher
matrix, no degeneracy
between other
parameters.



IM is a powerful tool to explore high- z Universe!

Thanks!