

Cosmology on Safari

Void properties in $f(R)$ gravity

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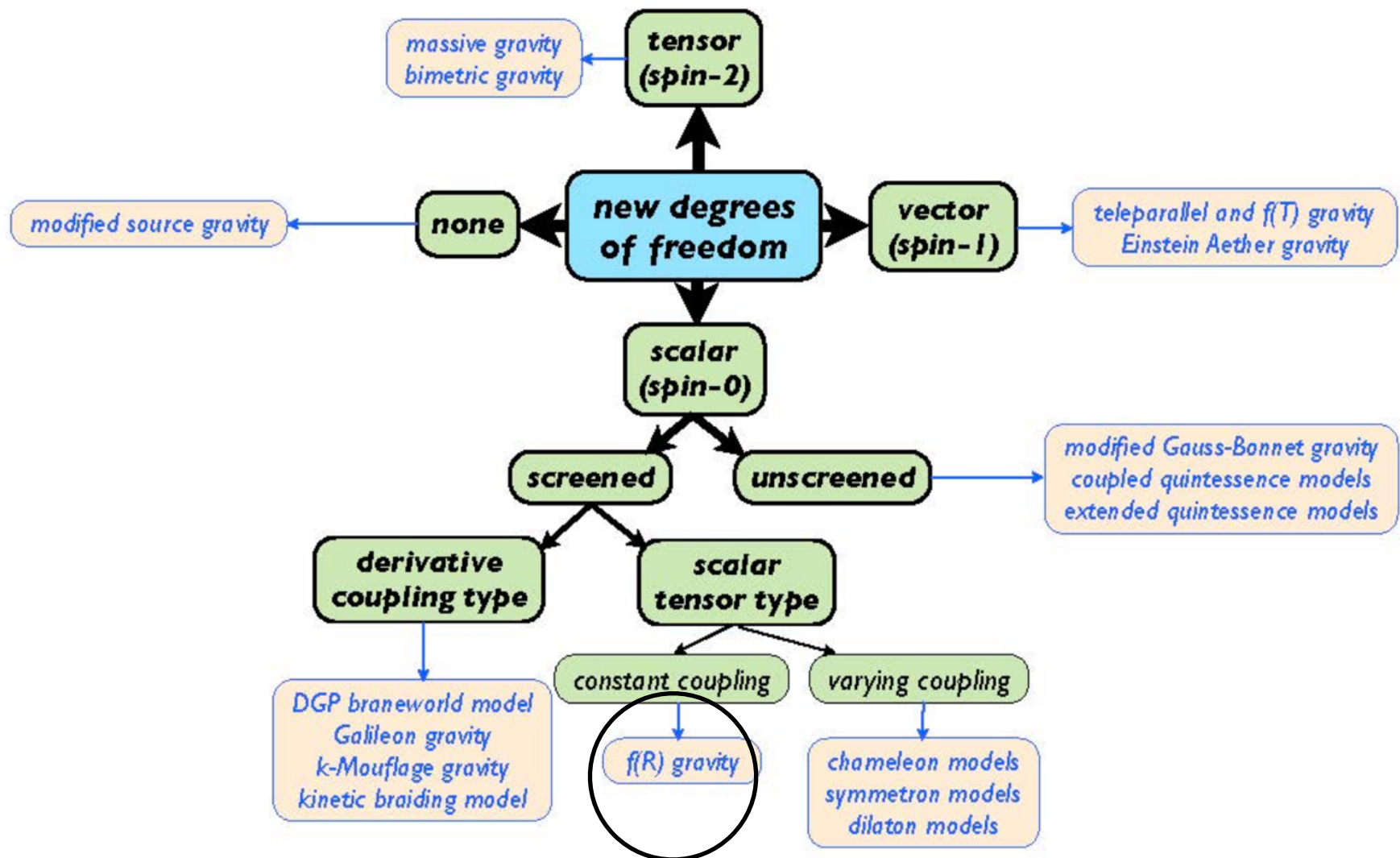
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Cai, Padilla & Li, arXiv:1410.1510

Outline

- ▶ Modified Gravity (MoG) and $f(R)$
- ▶ Abundance and large scale DM profiles:
MoG, tensions in Λ CDM
- ▶ MoG simulations
- ▶ MoG-void connection
- ▶ GR or MoG? void abundances and profiles:
density and lensing. arXiv:1410.1510

MoG



Courtesy Baojiu Li

MoG

- ▶ Modified gravity (MoG) models can explain the accelerating expansion **without a cosmological constant**.
- ▶ Scalar field coupled to matter (consistent with $f(R)$ models) or extra term in Einstein-Hilbert action trigger extra **fifth force** that enhances gravity.
- ▶ Screening mechanism that suppresses fifth force in high density regions is needed to make observationally viable theory.
- ▶ Fifth force is screened in early universe (CMB is unchanged) and in high density regions (Solar system).

f(R) MOG

Replace cosmological constant by $f(R)$ in the action, but ensure screening mechanism and GR where tested already:

$$S = \int d^4x \sqrt{-g} \left[\frac{1}{2} M_{\text{Pl}}^2 (R + f(R)) + \mathcal{L}_m \right]$$

Hu-Sawicki $f(R)$ model:
$$f(R) = -M^2 \frac{c_1 (-R/M^2)^n}{c_2 (-R/M^2)^n + 1}$$

where
$$\frac{c_1}{c_2} = -\frac{1}{n} \left[3 \left(1 + 4 \frac{\Omega_\Lambda}{\Omega_m} \right) \right]^{1+n} f_{R0}$$

and the characteristic mass M satisfies
$$M^2 = 8\pi G \bar{\rho}_{m0} / 3 = H_0^2 \Omega_m$$

Cluster abundance data constrain: $|f_{R0}| \lesssim 10^{-4}$ for $n=1$ (Schmidt et al. 2009).
This is the chameleon parameter.

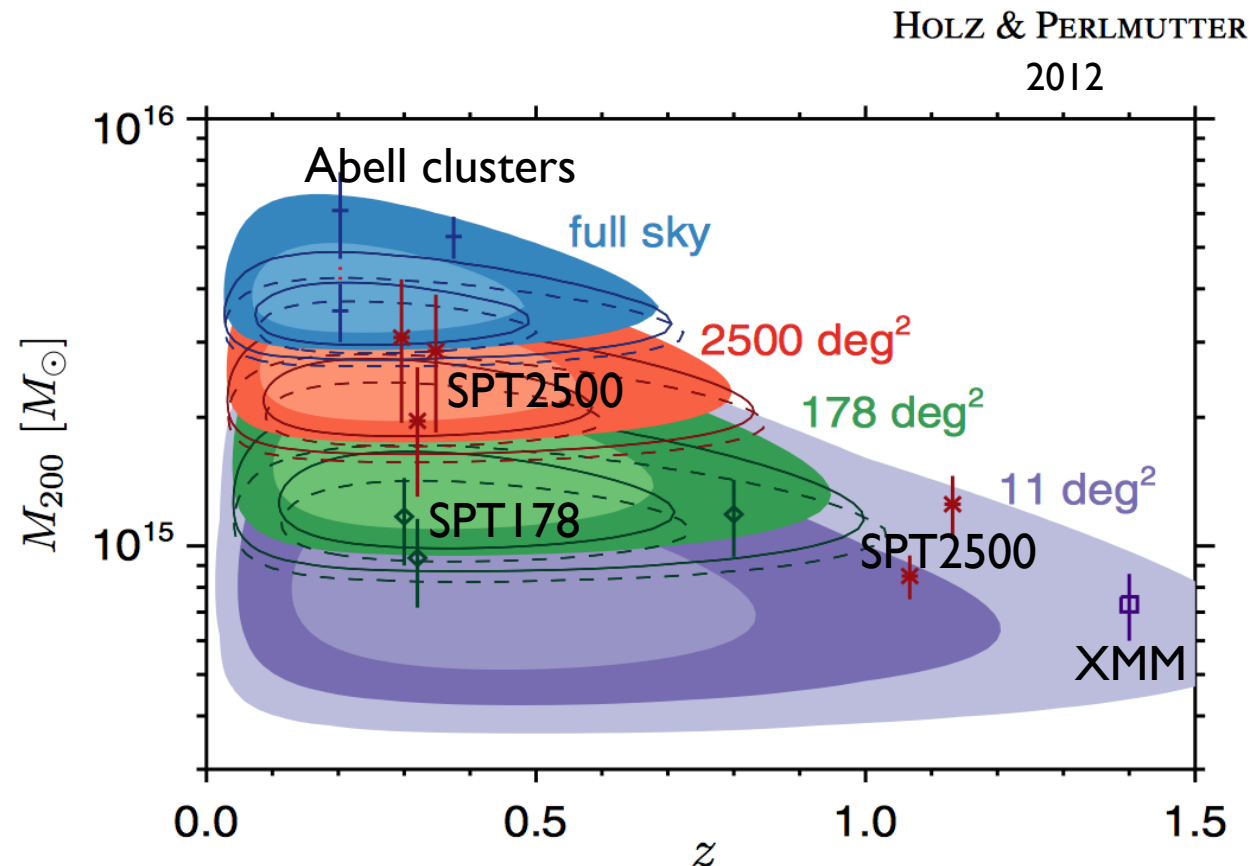
Also with other observables: Jennings et al. (2012), Hellwing et al. (2013)

MoG and LCDM

► Due to fifth force haloes grow faster in MoG and are more massive and abundant in these models (Li et al., 2012).

► Some tension with LCDM on the masses of the more massive clusters (El Gordo, Jack's talk).

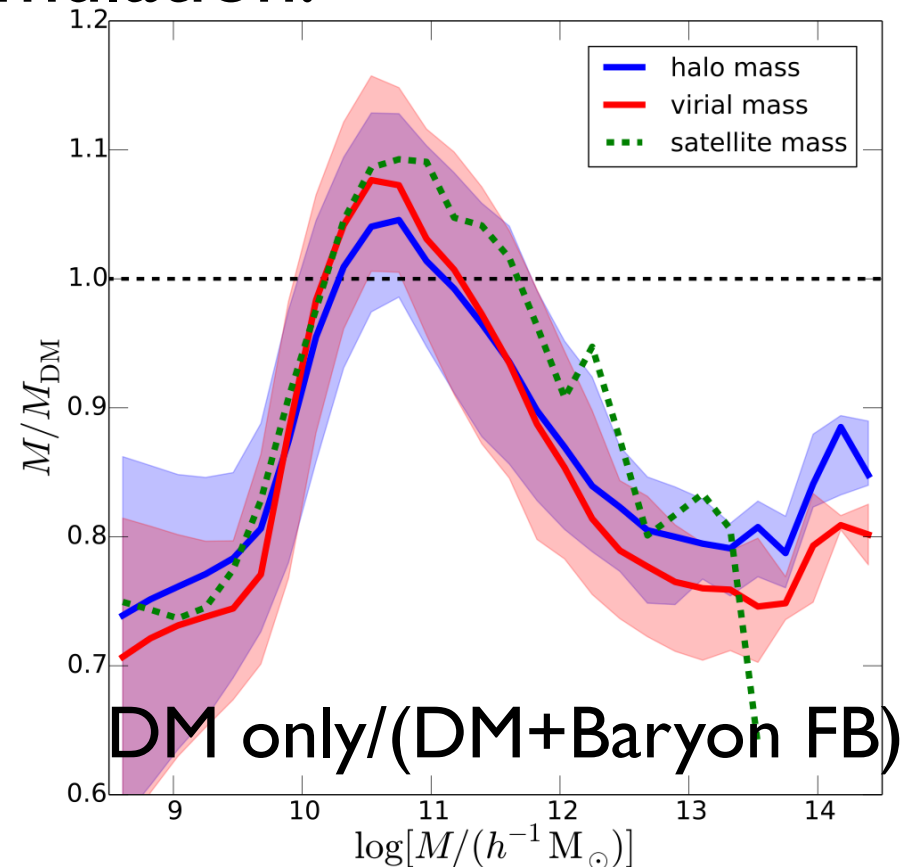
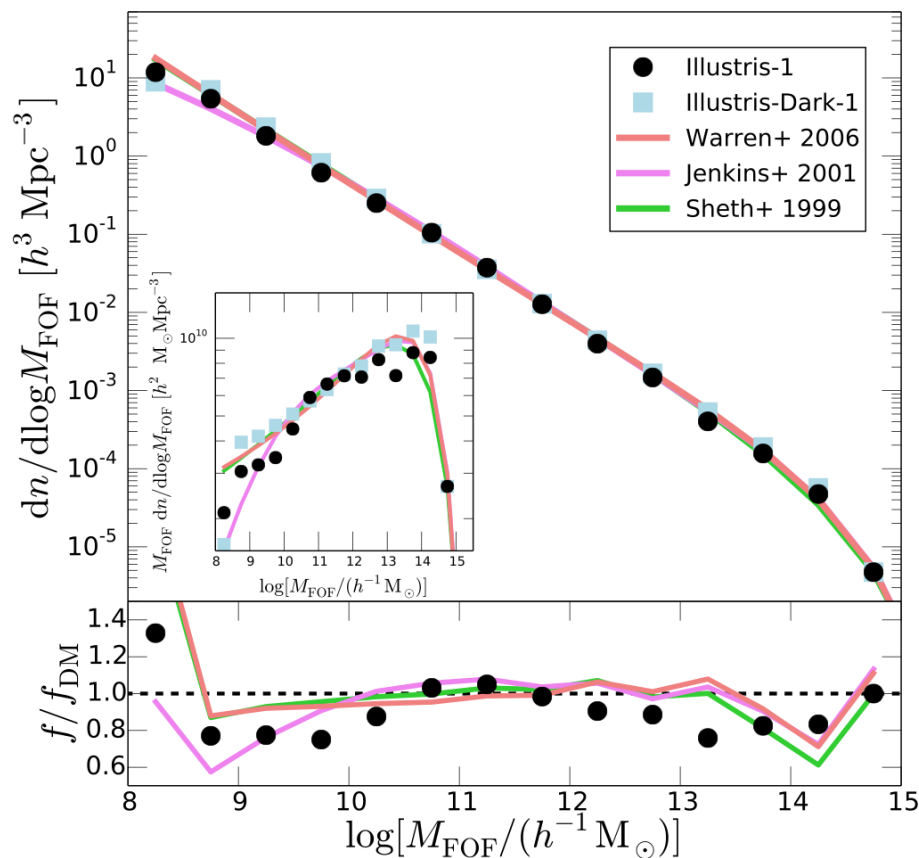
► However, analyses using extreme value statistics (e.g. Harrison & Coles 2012) seem to indicate this is actually not a problem.



MoG and LCDM

► But high mass end could be overestimated because baryons are not included: increased tension for LCDM.

Illustris simulation:



Volkersberger et al. 2014

Too big to fail problem

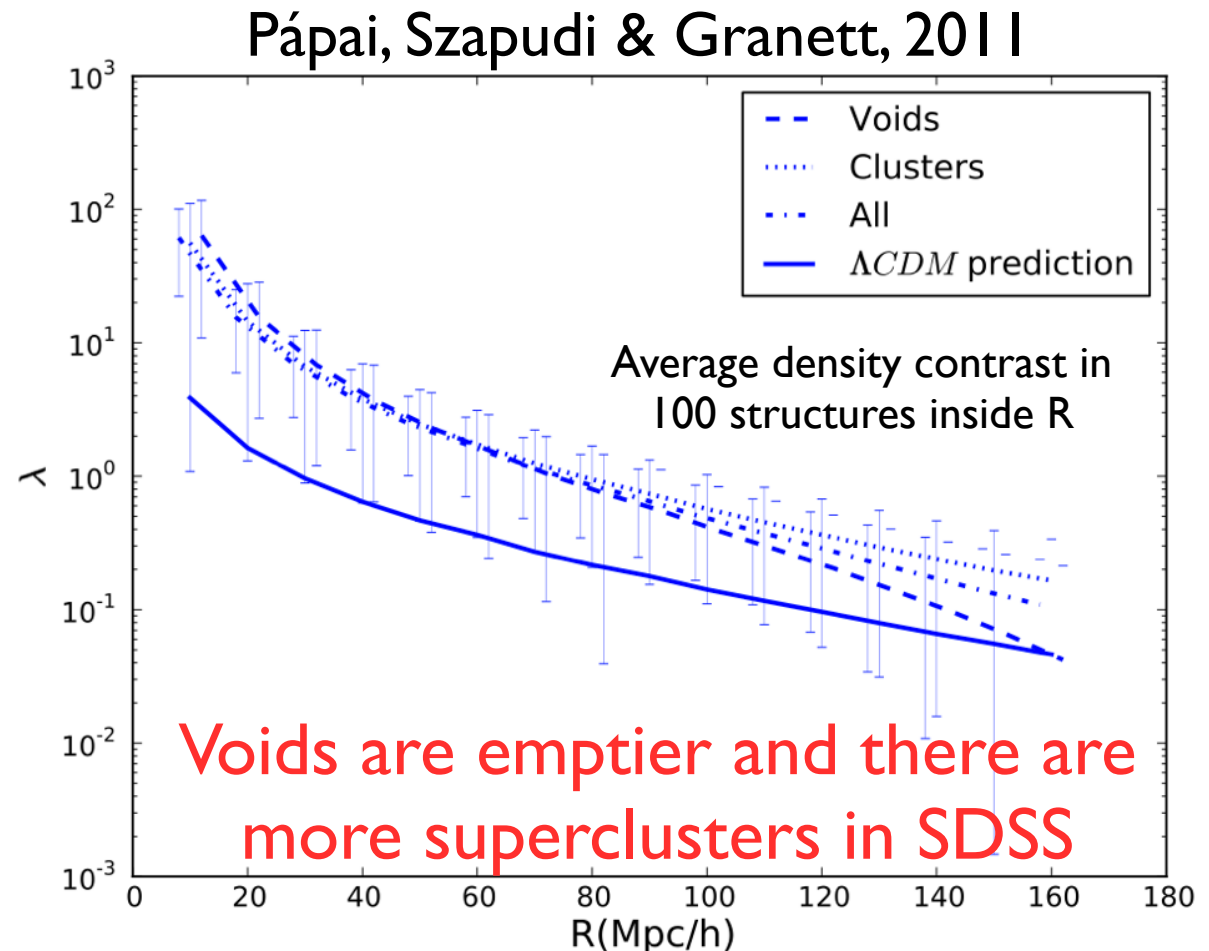
- ▶ Strong tension in masses of satellites: influenced by inner density profile of DM haloes. Unresolved issue.
- ▶ Another possible solution: WDM but complicated to simulate due to numerical stabilities that produce spurious low mass objects.

LCDM and MoG-void connection

► Further tension from Integrated Sachs-Wolfe effect (ISW).

► Pápai et al. find a 2-sigma difference in measurement from SDSS superstructures (superclusters and voids) and LCDM

► Nadathur, Hodgkiss & Sarkar (2013) include systematics (using largest voids only) and find discrepancy of 3sigma.



Similar conclusions by Flender et al. 2012, Hernandez-Monteagudo & Smith 2012

Non-linear problem

MoG simulations: f(R)

Hu-Sawicky f(R) model: $f(R) = -M^2 \frac{c_1 (-R/M^2)^n}{c_2 (-R/M^2)^n + 1}$ where $\frac{c_1}{c_2} = -\frac{1}{n} \left[3 \left(1 + 4 \frac{\Omega_\Lambda}{\Omega_m} \right) \right]^{1+n} f_{R0}$
 and the characteristic mass M satisfies $M^2 = 8\pi G \bar{\rho}_{m0}/3 = H_0^2 \Omega_m$

Cluster abundance data constrain: $|f_{R0}| \lesssim 10^{-4}$ for $n=1$ (Schmidt et al. 2009). This is the chameleon parameter.

Also with other observables: Jennings et al. (2012), Hellwing et al. (2013)

The equations needed for the N-body simulation are (Jennings et al., 2012):

$$\nabla^2 f_R = -\frac{1}{3}a^2 [R(f_R) - \bar{R} + 8\pi G (\rho_m - \bar{\rho}_m)] \quad \nabla^2 \Phi = \frac{16\pi G}{3}a^2 (\rho_m - \bar{\rho}_m) + \frac{1}{6}a^2 [R(f_R) - \bar{R}]$$

Simulations from Zhao, Li & Koyama, 2012: ECOSMOG code (Li et al. 2012)
 based on RAMSES (Teyssier 2002)

GR and f(R) models start from the same initial conditions.

MoG simulations: f(R)

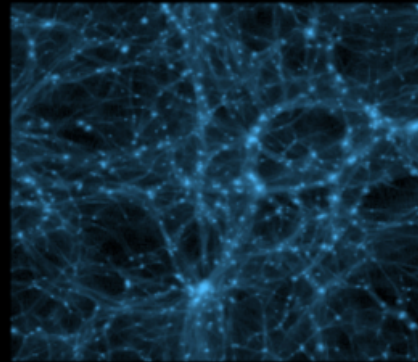
WMAP7 cosmology:

$$\{\Omega_m, \Omega_\Lambda, n_s, h \equiv H_0/(100\text{km/s/Mpc}), \sigma_8\} = \{0.24, 0.76, 0.961, 0.73, 0.80\}$$

Models	$L_{\text{box}} (h^{-1} \text{ Gpc})$	Particles	Domain meshes	Finest meshes	Convergence criterion	Realizations
$\Lambda\text{CDM, F6, F5, F4}$	1.0	1024^3	1024^3	65536^3	$ \epsilon < 10^{-12}/10^{-8}$	1
$\Lambda\text{CDM, F6, F5, F4}$	1.5	1024^3	1024^3	65536^3	$ \epsilon < 10^{-12}/10^{-8}$	6

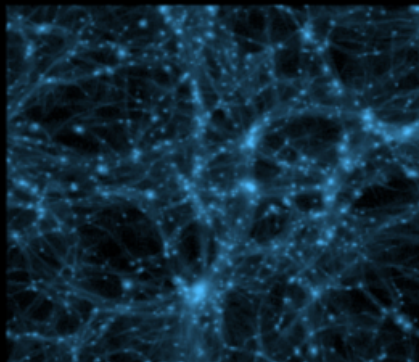
Analysis
centred on
1 Gpc³ volume
(SDSS LRG size)

GR

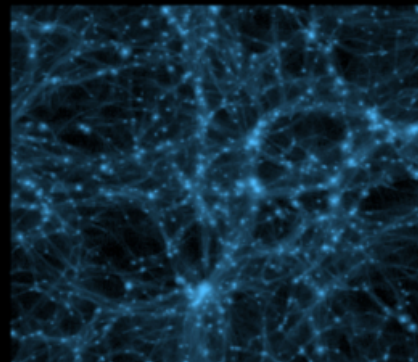


[Gong-Bo Zhao](#)

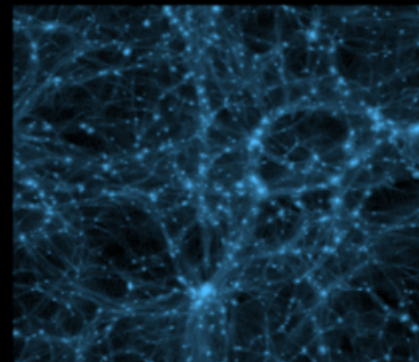
F4: $|f_{R0}| = 10^{-4}$ No-Ch



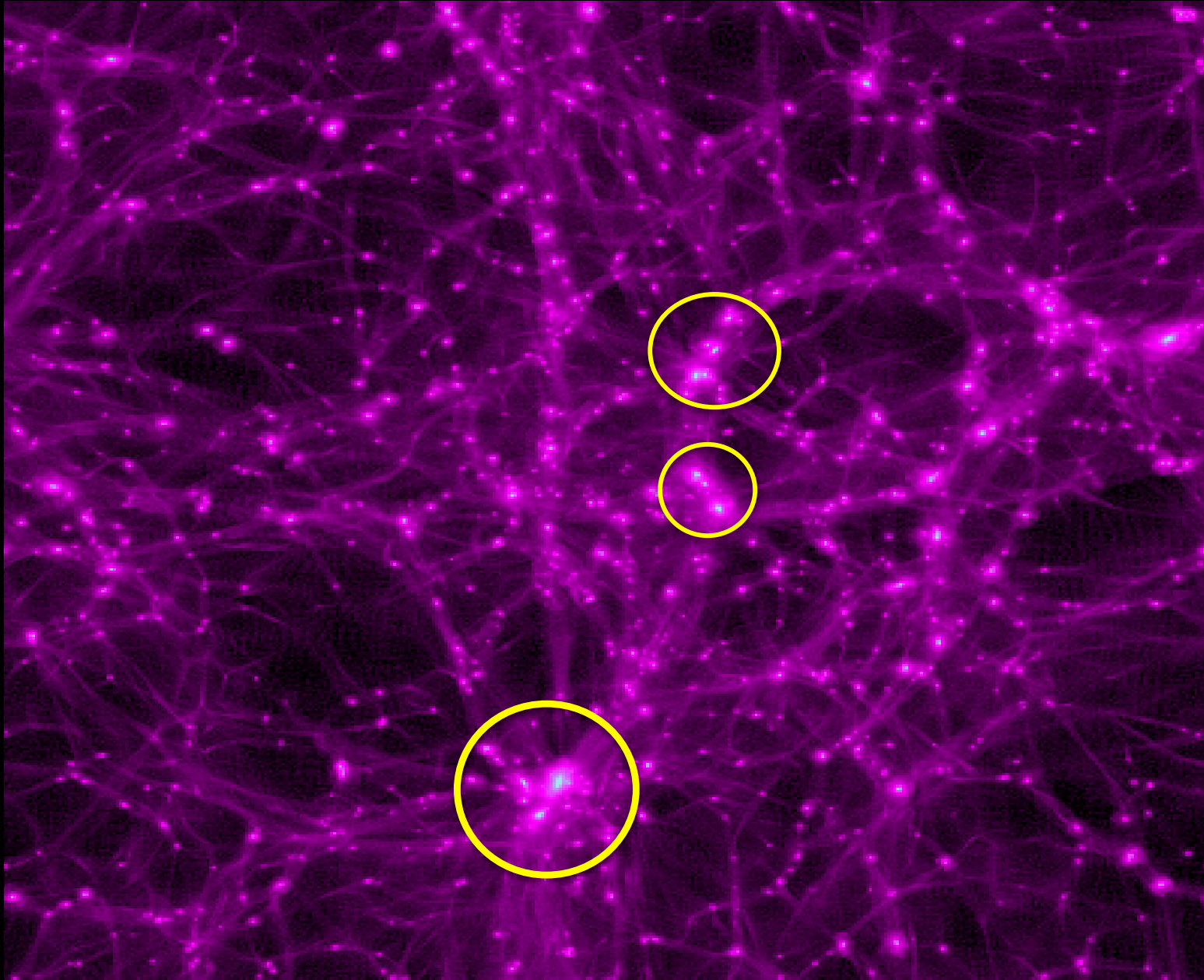
F5: $|f_{R0}| = 10^{-5}$



F6: $|f_{R0}| = 10^{-6}$ Full-Ch

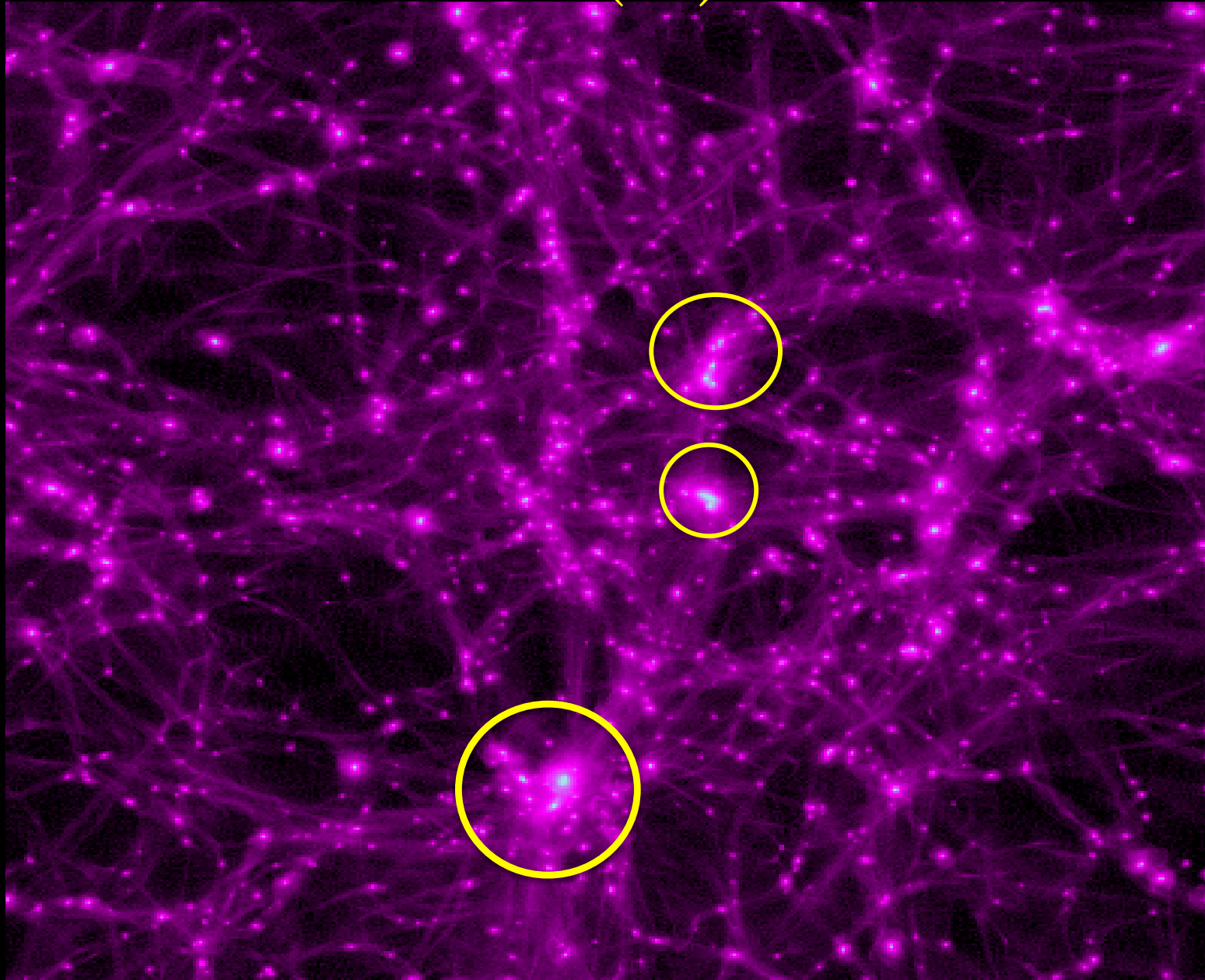


GR



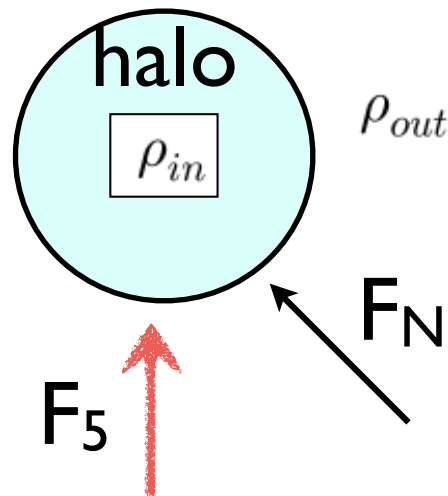
Gong-Bo Zhao

$f(R)$



Gong-Bo Zhao

Halo and the fifth force



► Positive fifth force outside haloes acting in addition to newtonian.

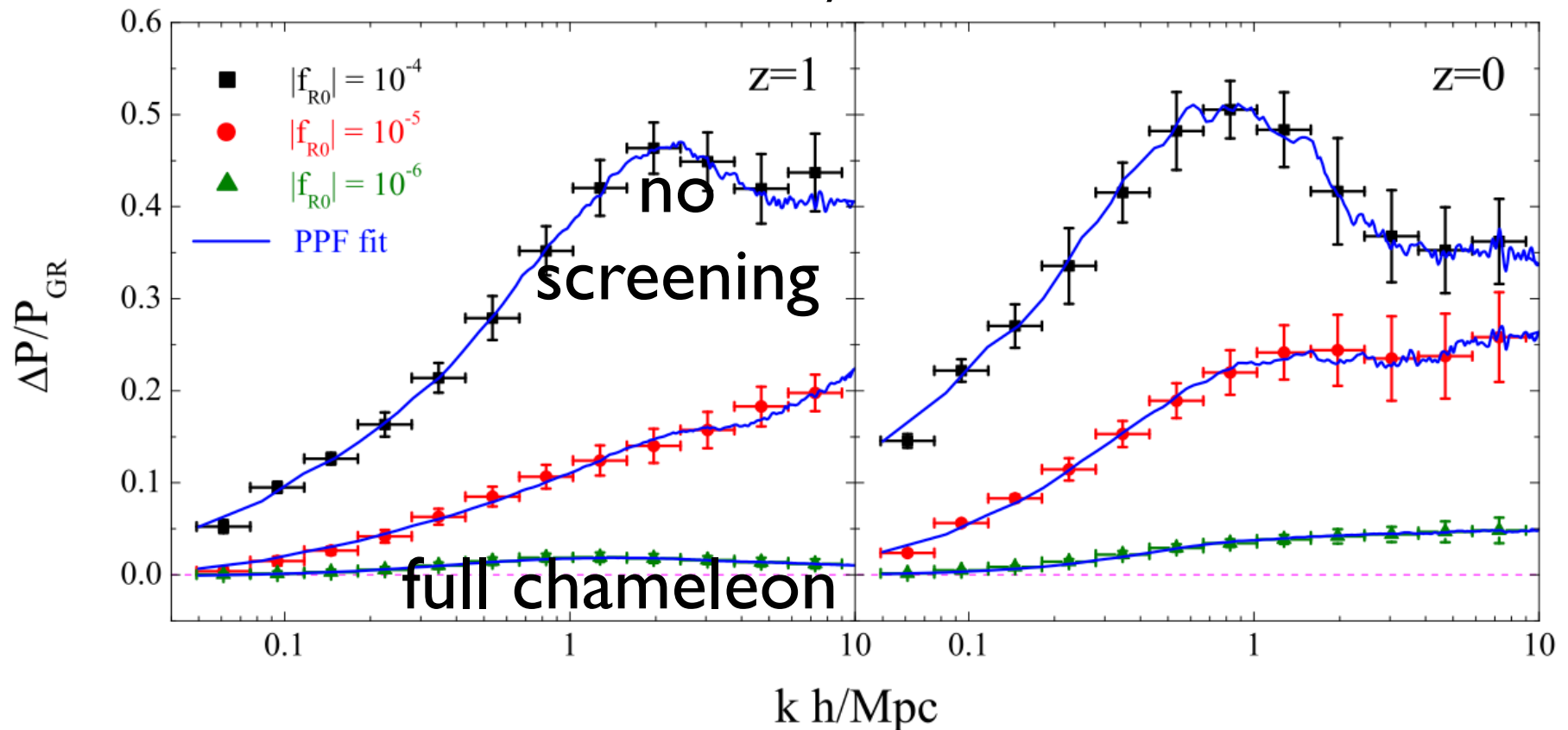
► Effect present at low masses.

► At high masses effect increases for high fifth force strength parameter.

Could reconcile El Gordo more easily
Could help with the too big to fail problem

MoG simulations: $f(R)$

Power spectra:
Zhao, Li & Koyama, 2012



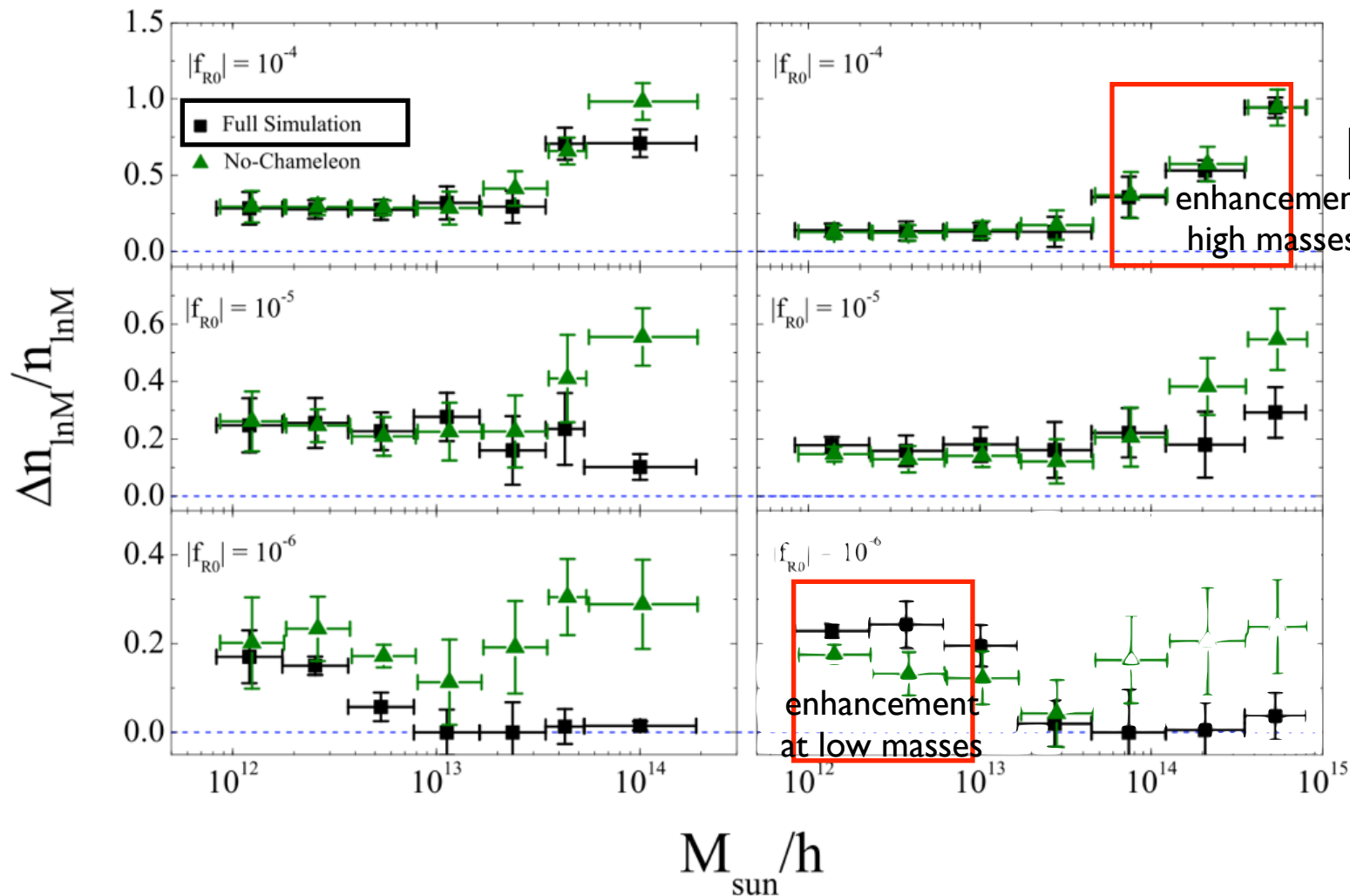
Non linear power increased ($\sim$ l-halo term)

MoG simulations: $f(R)$

Mass functions:
Zhao, Li & Koyama, 2012

$z=1$

$z=0$



No screening

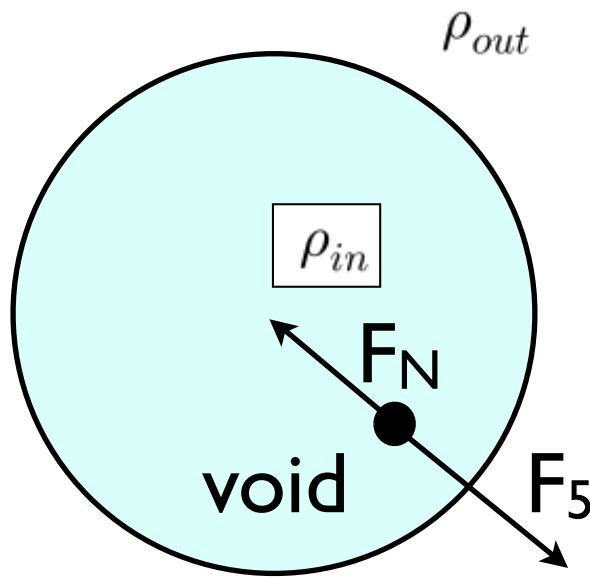
Intermediate
screening

Full
Chameleon

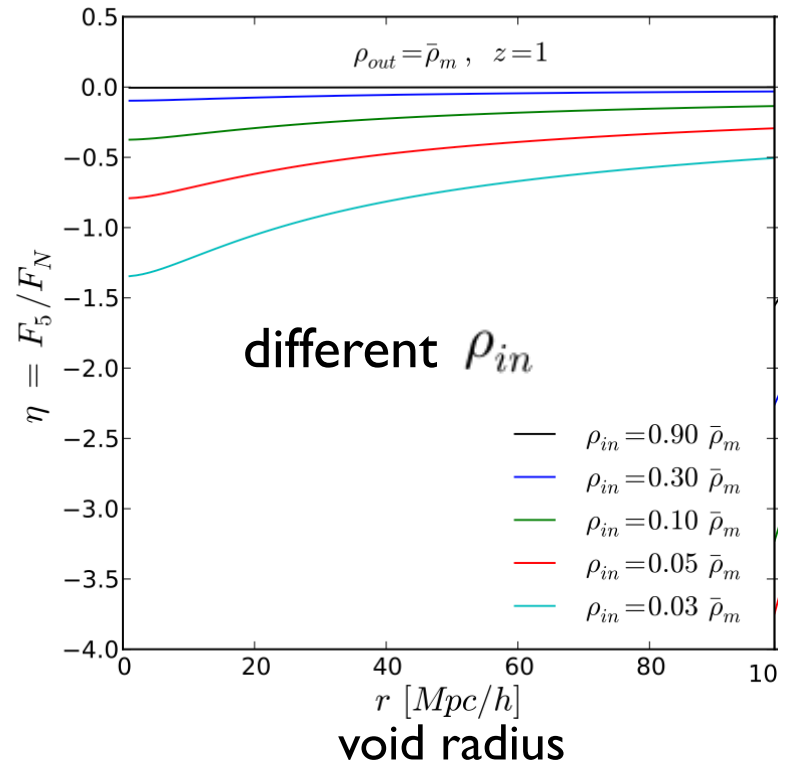
MoG-void connection

Voids are emptier in SDSS

► Clampitt et al. 2013 calculate the fifth and newtonian forces for a top-hat void.

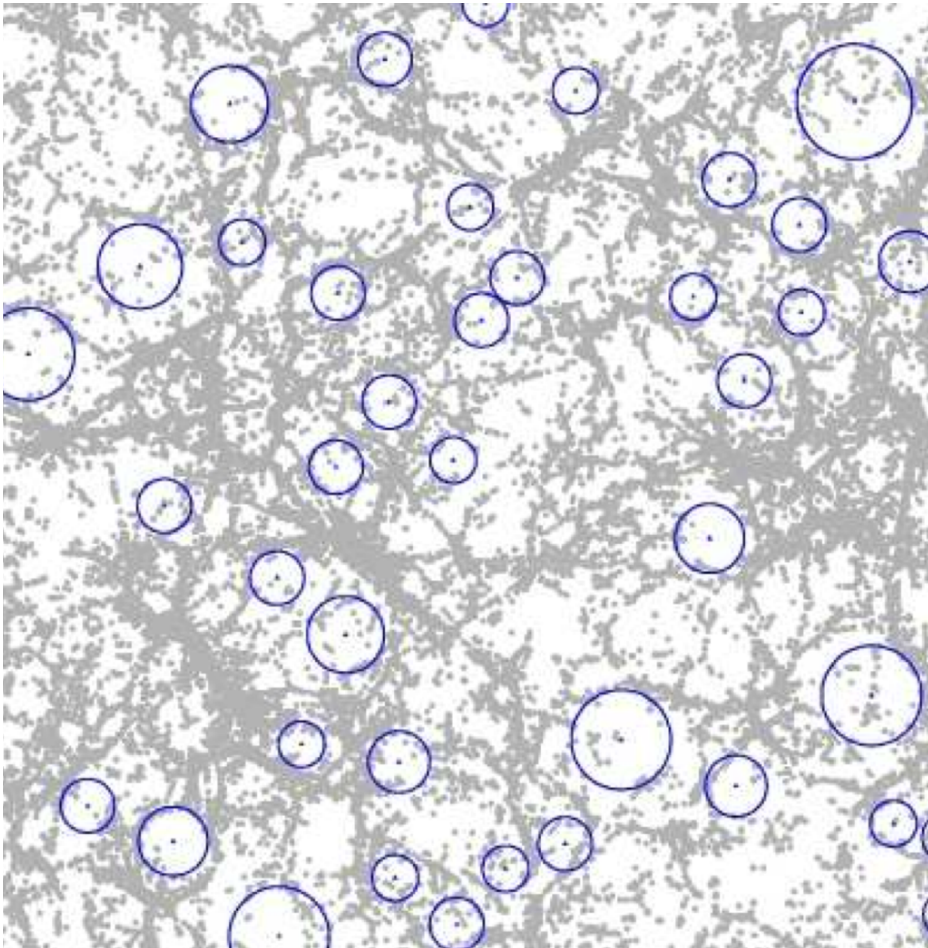


Negative fifth force inside voids acting in opposite direction to newtonian. Stronger for lower internal density, and for small voids.

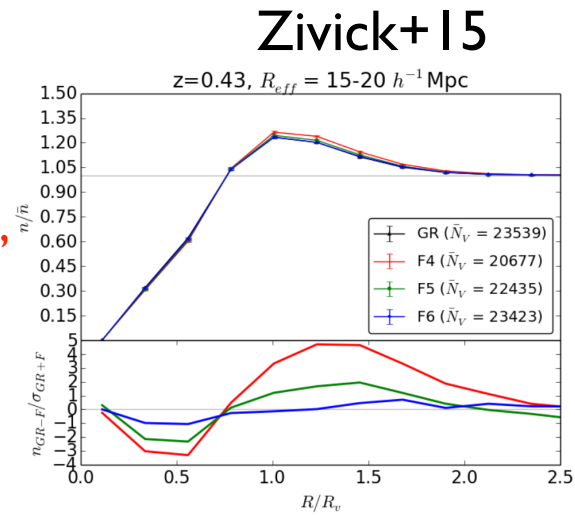


Identifying voids

mP05



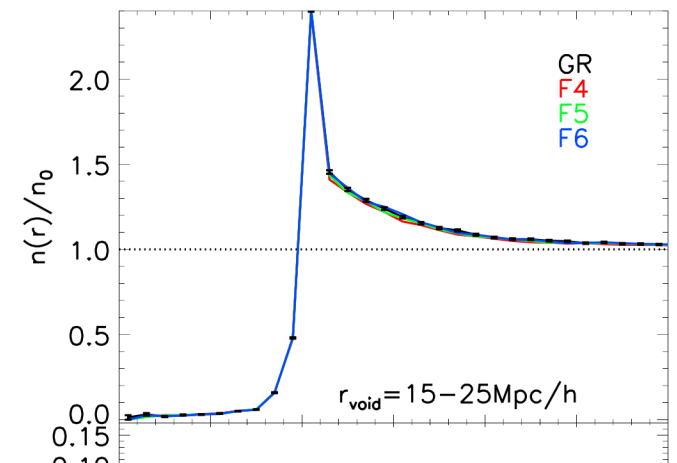
► ZOBOV, Watershed, VIDE,...: slow transition to average density.



► mP05 (modified Padilla et al. 2005, MNRAS 363, 977): largest spheres with **integrated density**

$$\rho_{\min}/\bar{\rho} < 0.2.$$

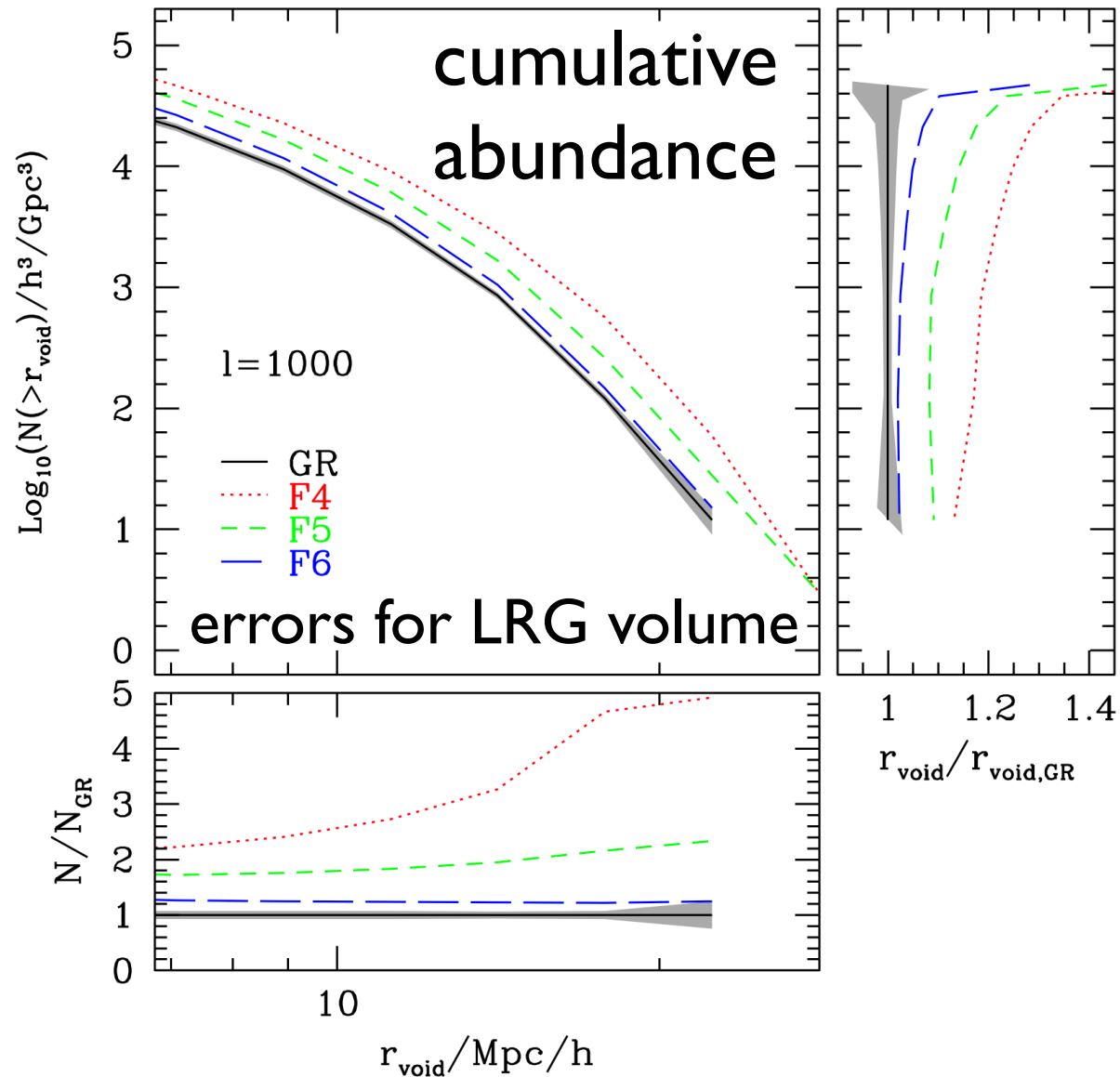
Fast transition to average density.



Void abundances

mP05 void abundances in $f(R)$ simulations and GR.

25% difference between F6 and GR (highly significant), and up to x3 factor for F4 is promising!



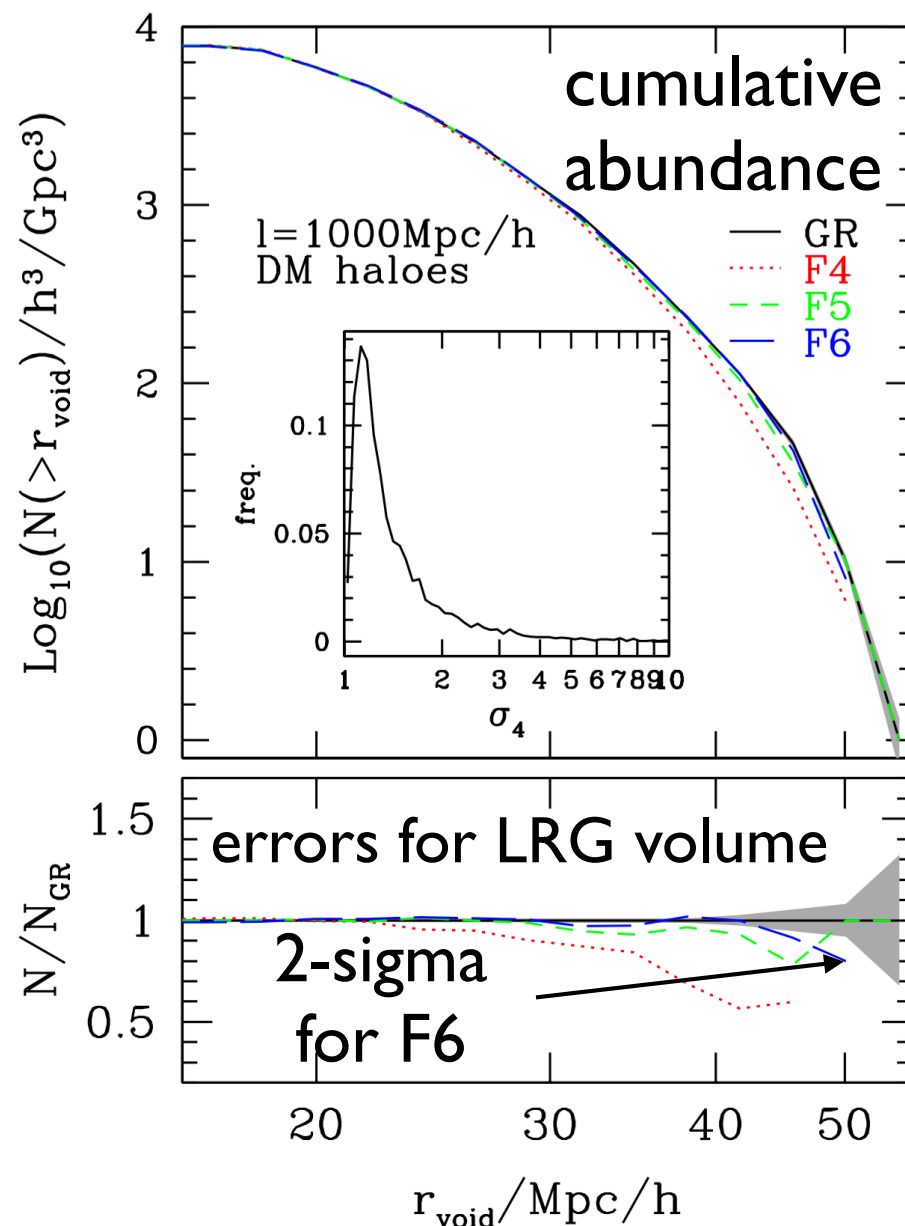
- ▶ Zivick, Sutter et al. (arXiv:1411.5694) predict consistent differences for EUCLID voids, matching space density of future samples.
- ▶ However, they randomly sample a fraction of dark matter particles in the simulation instead of using biased tracers of the density field.

Void abundances for biased tracers

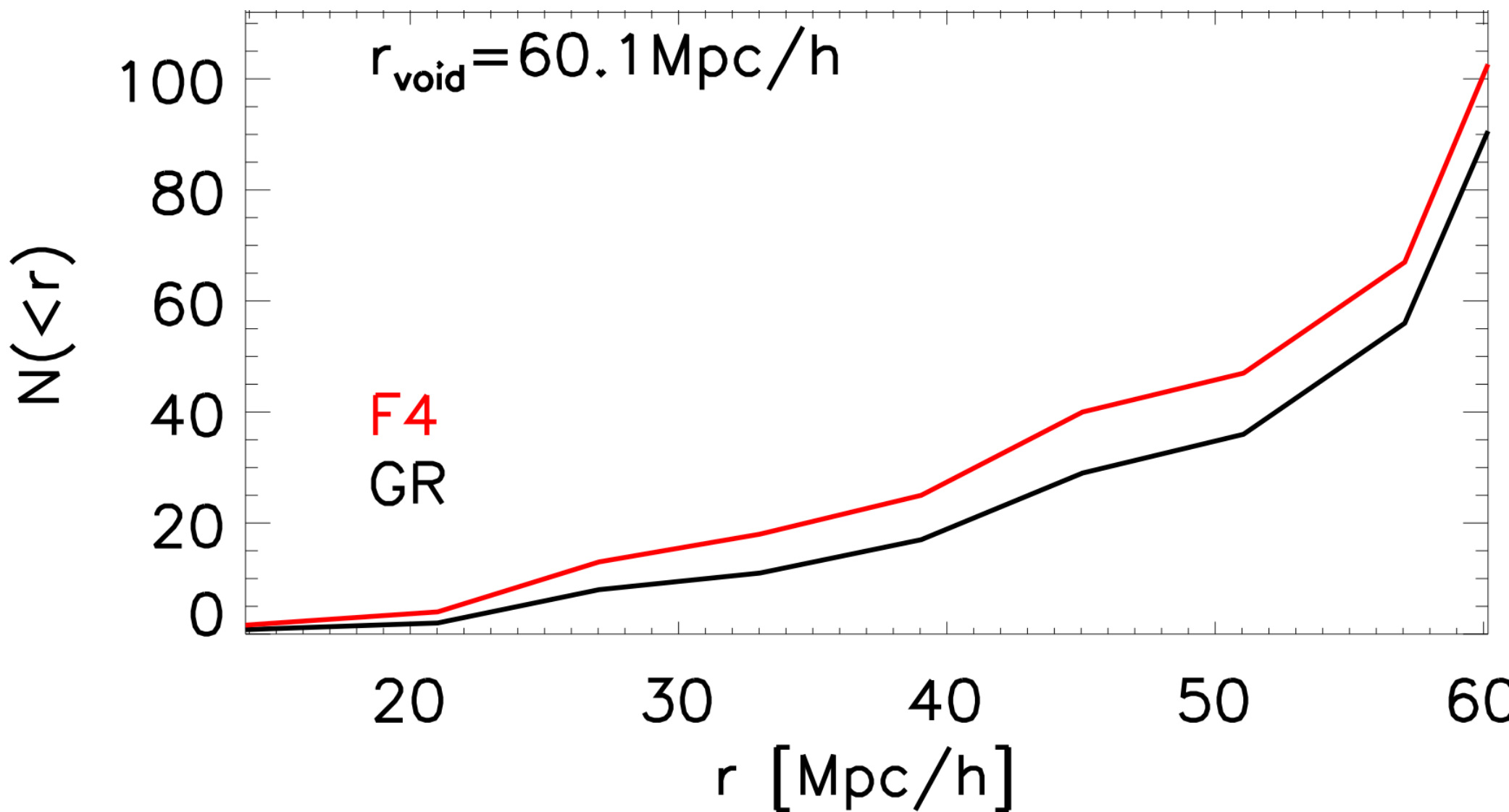
mP05 void abundances in $f(R)$ simulations and GR.

Behaviour is reversed.

Differences are smaller and depend on radius of void when tracers are used.



Profile around GR centre of the largest void:

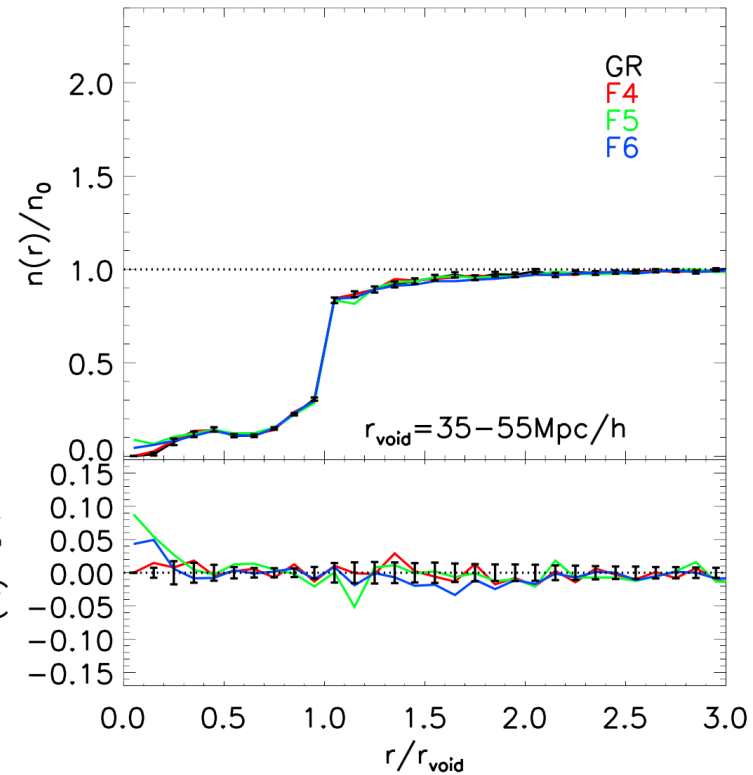
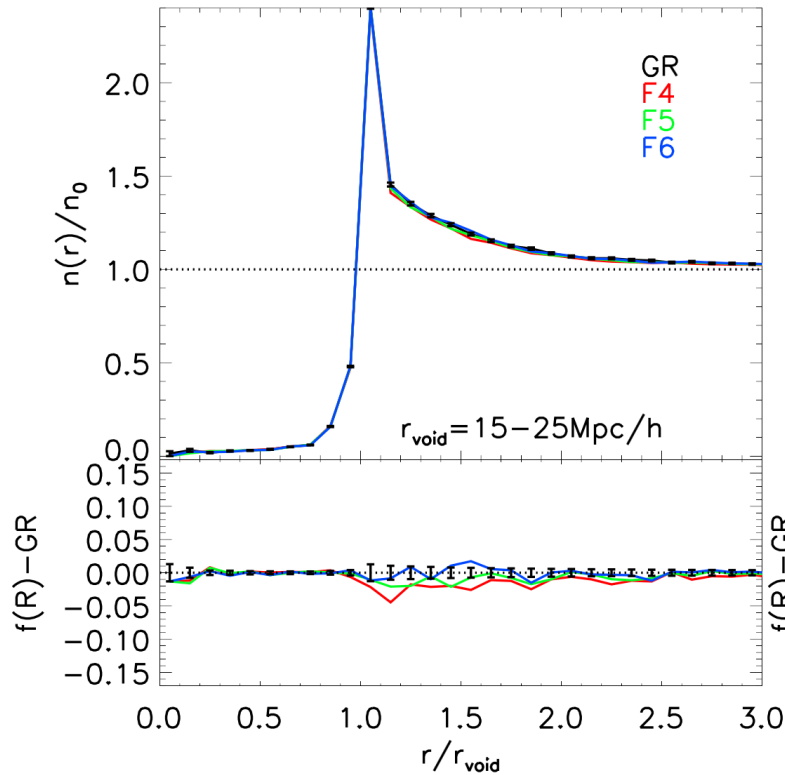


There are more haloes in F4 inside the void.

CPL, arXiv:1410.1510

Stacked void profiles

Differential profiles
traced by **haloes**.



Voids identified
using haloes

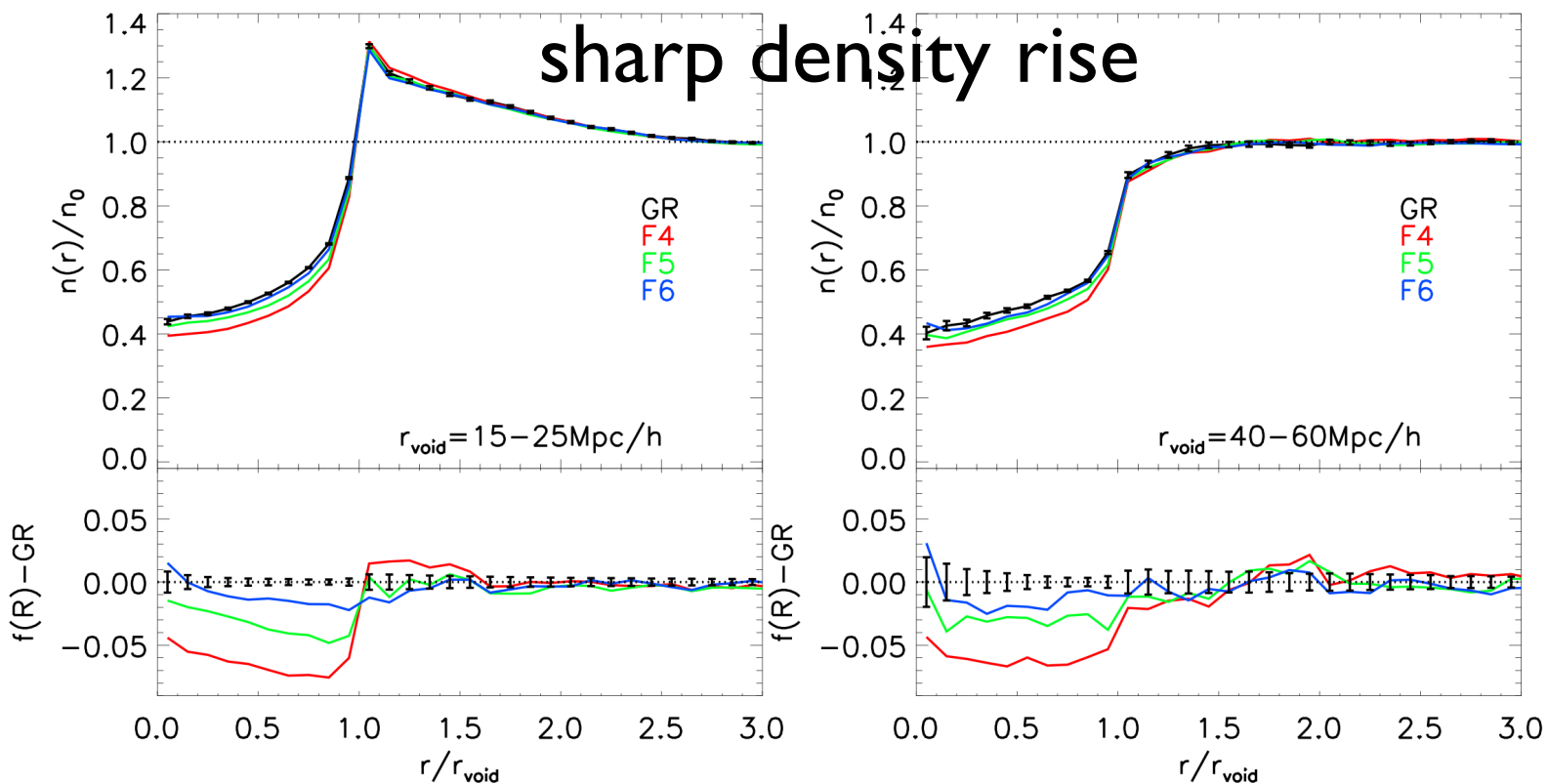
Because of the way halos form in $f(R)$ models, the stacked profiles only show mild differences:

less pronounced ridges in $f(R)$

CPL, arXiv:1410.1510

Stacked void profiles

Differential profiles
traced by **DM**.



Voids identified
using haloes

DM profiles confirm emptier voids in $f(R)$ models even
if halo density is the same.

But how to measure **DM** profiles around halo defined voids?

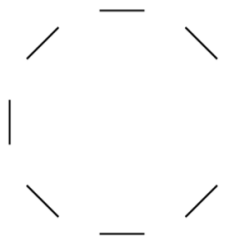
CPL, arXiv:1410.1510

Lensing profiles

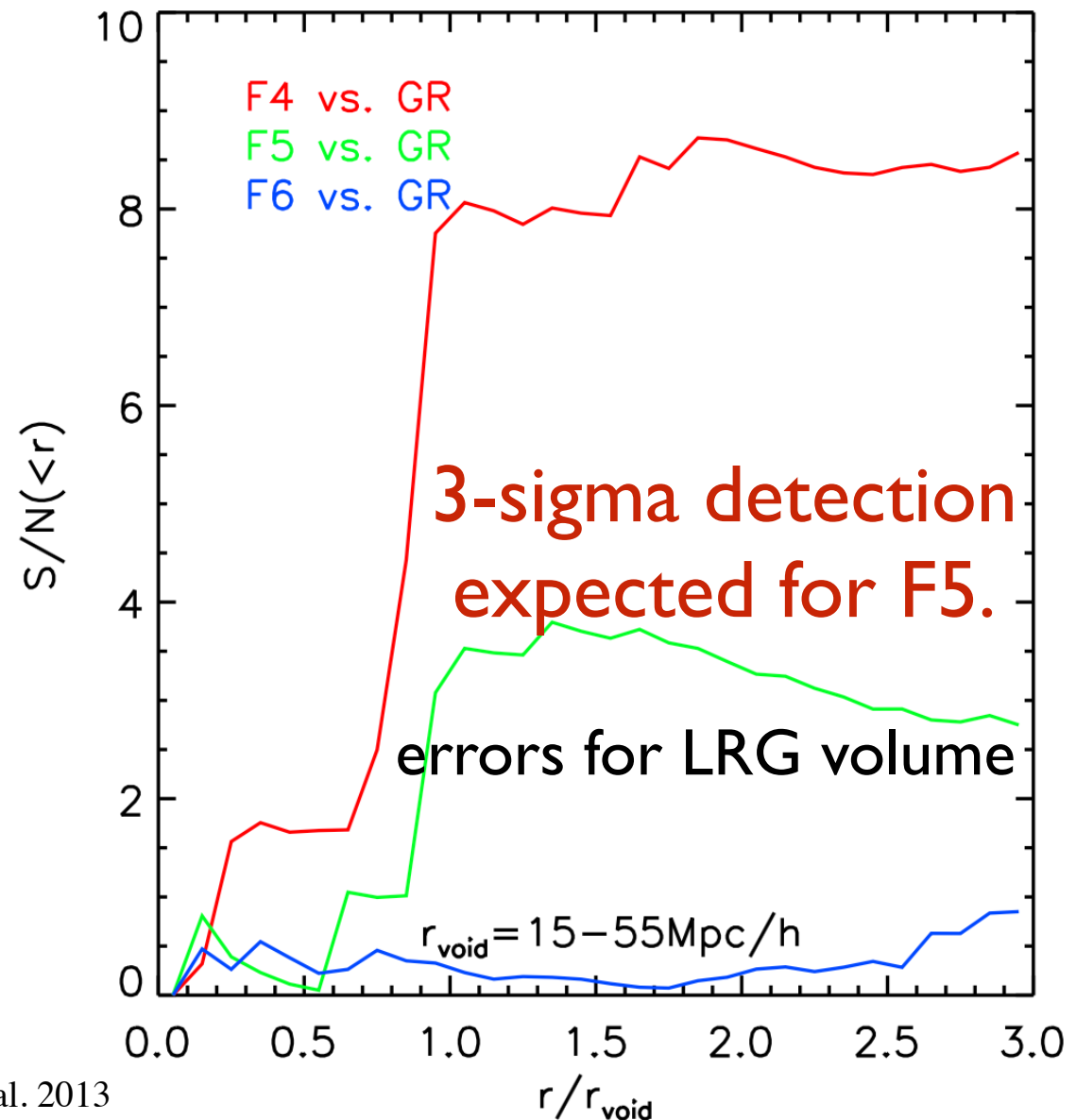
Derivative of the
3D density profile
around mP05
voids as analog of
the tangential
shear profile.

$$\Delta\Sigma(R) = \gamma_t \Sigma_c = \Sigma(< R) - \Sigma(R),$$

$$\Sigma_c = \frac{c}{4\pi G} \frac{D_A(z_s)}{D_A(z_l) D_A(z_l, z_s) (1 + z_l)}.$$



CPL, arXiv:1410.1510



Conclusions

- ▶ The Λ CDM model is extremely successful yet there are tensions: larger small haloes (TBTF), emptier voids (ISW), more massive superclusters (ISW), massive clusters at high- z . Voids can provide high signal to noise to detect $f(R)$ gravity.
- ▶ Strong variation in significance of comparison between GR and $f(R)$ depending on whether the mass or a tracer is used to detect/analyse voids.
- ▶ Voids provide many plausible tests involving:
 - ▶ abundance of tracer voids for large void sizes,
 - ▶ density profiles of voids if mass is used,
 - ▶ lensing by voids is a good way to trace profiles using the mass.
 - ▶ Combination of abundance+lensing profiles

$f(R)$ simulations
of 1 Gpc^3
1/6th that of
BOSS DR11

Thank you